

Rotationally Invariant Slave-Boson and application in combination with Density Functional Theory

Nicola Lanatà (MagLab)

Assistant for Hands-on Session: Tsung-Han Lee

E-mail: lanata@magnet.fsu.edu



LECTURE

RISB formalism, numerical implementation and application in combination with DFT

N. Lanatà, Y. Yao, X. Deng, V. Dobrosavljevic and G. Kotliar, arXiv:1606.09614 (2016)

N. Lanatà, Y. Yao, C.-Z. Wang, K.-M. Ho, and G. Kotliar, PRX **5**, 011008 (2015)

N. Lanatà, H. U. R. Strand, X. Dai and B. Hellsing, Phys. Rev. B, **85**, 035133 (2012)

N. Lanatà, P. Barone and M. Fabrizio, Phys. Rev. B **78**, 155127 (2008)

F. Lechermann, A. Georges, G. Kotliar, and O. Parcollet, PRB **76**, 155102 (2007)

HANDS-ON SESSION

(assistant: **Tsung-Han Lee**)

Using RISB Code Developed with
Yongxin Yao (Iowa) and Gabriel Kotliar (Rutgers)

Implementation of LAPW interface with the DFT
WIEN2K code adapted from DFT+DMFT code of:
K. Haule et al., see Phys. Rev. B **81**, 195107 (2010).



LECTURE OUTLINE:

Introduction (what is DFT+RISB useful for?)

Operatorial Formulation Rotationally Invariant Slave Boson (RISB)

- The Single-Band Hubbard Model
- Slave Boson representations Hubbard Hamiltonian
- Slave Boson Mean Field Approximation

Algorithms and Implementation RISB mean field theory

- Functional Formulation
- Stationarity Equations and Numerical Implementation

DFT + Slave Boson Approximation (DFT+RISB)

- The correlated orbitals
- DFT+RISB: Solving iteratively Kohn-Sham-Hubbard model
- Examples: low-symmetry systems (UO_2), polymorphism

Reference system to describe strongly-correlated materials (determined from K.S.)

Generic multi-band Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{k}} \sum_{ij} \sum_{\alpha\beta} \epsilon_{\mathbf{k},ij}^{\alpha\beta} c_{\mathbf{k}i\alpha}^\dagger c_{\mathbf{k}j\beta} + \sum_{\mathbf{R}i \in \text{corr}} \hat{H}_i^{\text{loc}} [\{c_{\mathbf{R}i\alpha}^\dagger\}, \{c_{\mathbf{R}i\alpha}\}]$$

$$\epsilon_{\mathbf{k}} = \begin{bmatrix} i=0 & * & * \\ * & i=1 & * \\ * & * & i=2 \end{bmatrix}$$

R = label unit cell
k = Fourier-conjugate of **R**
 α, β = orbitals in **R**, i

(Example: $i = 0$: uncorrelated orbitals; $i = 1$: d orbitals atom 1
 $i = 2$: f orbitals atom 2 ...)

What is RISB/GA good for?

RISB (mean field) Theory / GA

- Non-perturbative many-body technique which can be viewed as a (“good”) approximation to DMFT.
- Largely complementary to DMFT because it is much less computationally demanding.

(The general RISB theory (before mean-field approximation) is an exact reformulation of the many-body problem.)

What is RISB/GA good for?

RISB (mean field) Theory / GA



Materials Genome Initiative

www.whitehouse.gov/mgi

[About](#) | [Goals](#) | [Examples](#) | [News & Announcements](#) | [Federal Programs](#) | [External Stakeholder Activities](#) | [Contact Us](#)

To help businesses discover, develop, and deploy new materials twice as fast, we're launching what we call the Materials Genome Initiative. The invention of silicon circuits and lithium-ion batteries made computers and iPods and iPads possible -- but it took years to get those technologies from the drawing board to the marketplace. We can do it faster.

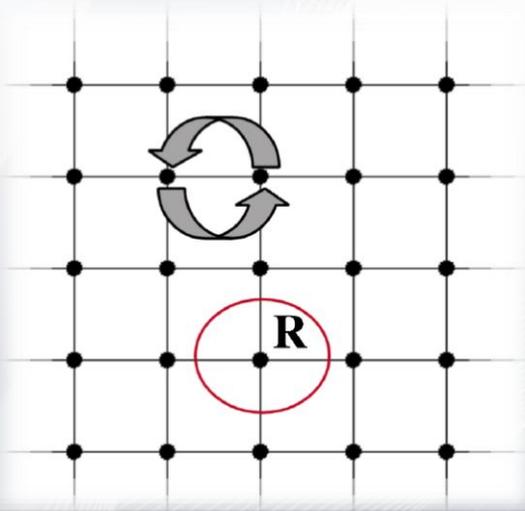
– President Obama, June 2011 at Carnegie Mellon University



Quadratic part correlated local orbitals included in \mathcal{H}^{loc}

The Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^{\dagger} c_{\mathbf{R}'\sigma} + \sum_{\mathbf{R}} U c_{\mathbf{R}\uparrow}^{\dagger} c_{\mathbf{R}\uparrow} c_{\mathbf{R}\downarrow}^{\dagger} c_{\mathbf{R}\downarrow}$$



\mathbf{R} = label site
 σ = spin = $\uparrow; \downarrow$
 U = Hubbard strength
 $\epsilon_{\mathbf{R}\mathbf{R}'}$ = hopping coefficients

$$\mathcal{H}_F = \otimes_{\mathbf{R}} \mathcal{H}_F^{\mathbf{R}} ; \quad \mathcal{H}_F^{\mathbf{R}} = \langle \{ |0, \mathbf{R}\rangle, | \uparrow, \mathbf{R}\rangle, | \downarrow, \mathbf{R}\rangle, | \uparrow\downarrow, \mathbf{R}\rangle, \} \rangle$$

$$= \langle \{ |0\rangle, c_{\mathbf{R}\uparrow}^{\dagger} |0\rangle, c_{\mathbf{R}\downarrow}^{\dagger} |0\rangle, c_{\mathbf{R}\uparrow}^{\dagger} c_{\mathbf{R}\downarrow}^{\dagger} |0\rangle \} \rangle$$

Focus on the local space at given \mathbf{R}

Local Hilbert Space



$$\begin{aligned}\mathcal{H}_F^{\mathbf{R}} &= \langle \{ |0, \mathbf{R}\rangle, | \uparrow, \mathbf{R}\rangle, | \downarrow, \mathbf{R}\rangle, | \uparrow\downarrow, \mathbf{R}\rangle, \} \rangle \\ &= \langle \{ |0\rangle, c_{\mathbf{R}\uparrow}^\dagger |0\rangle, c_{\mathbf{R}\downarrow}^\dagger |0\rangle, c_{\mathbf{R}\uparrow}^\dagger c_{\mathbf{R}\downarrow}^\dagger |0\rangle \} \rangle\end{aligned}$$

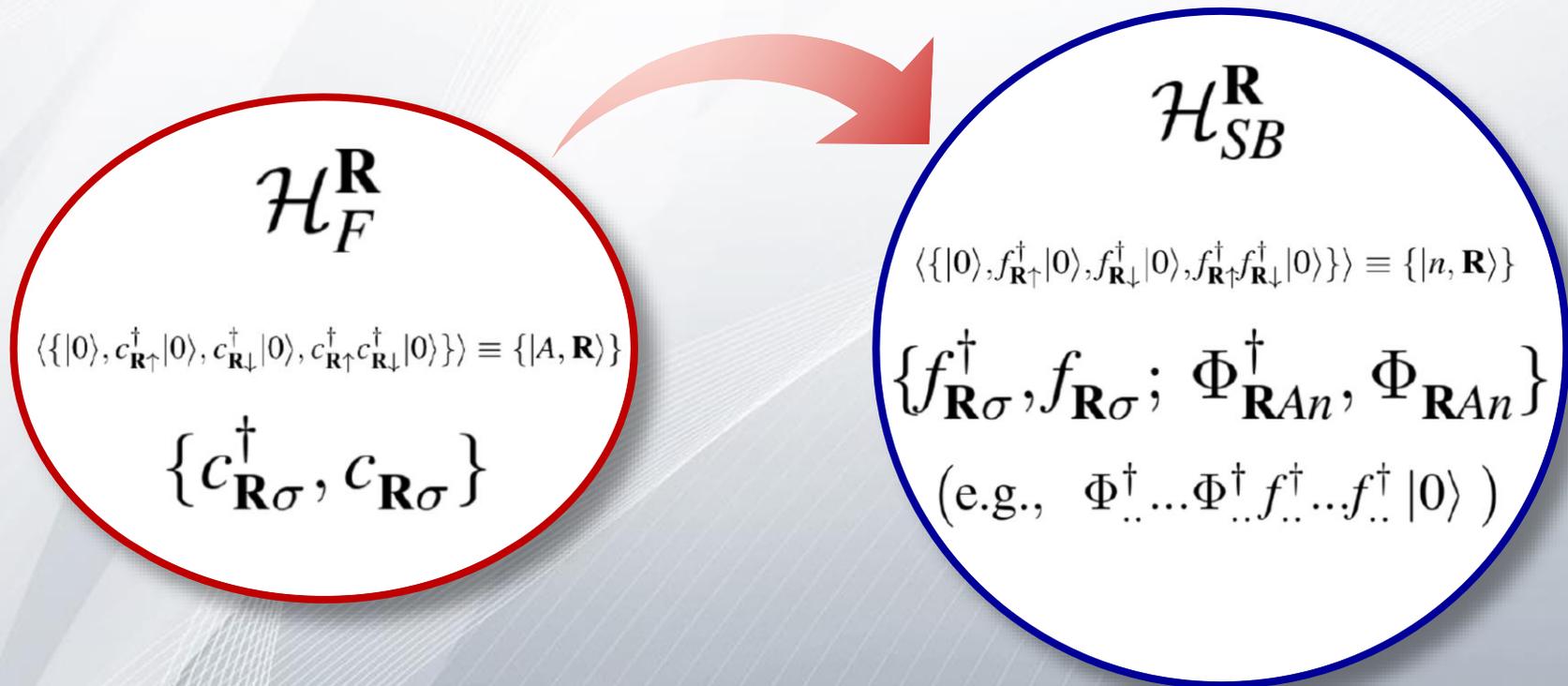
Define unitary map from Fermionic many-body local Fock space $\mathcal{H}_F^{\mathbf{R}}$ into bigger Hilbert space $\mathcal{H}_{SB}^{\mathbf{R}}$ (generated by “artificial” Bosonic and Fermionic degrees of freedom)

(Scope: derive equivalent reformulation of the Hubbard model more suitable to define a mean-field approximation)

Defining mapping onto subspace of infinite-dimensional Hilbert space

Slave-Boson Local Hilbert Space

\mathcal{H}_{SB}^R generated by “artificial” Bosonic and Fermionic degrees of freedom
 (dimension $\mathcal{H}_{SB}^R = \infty$)

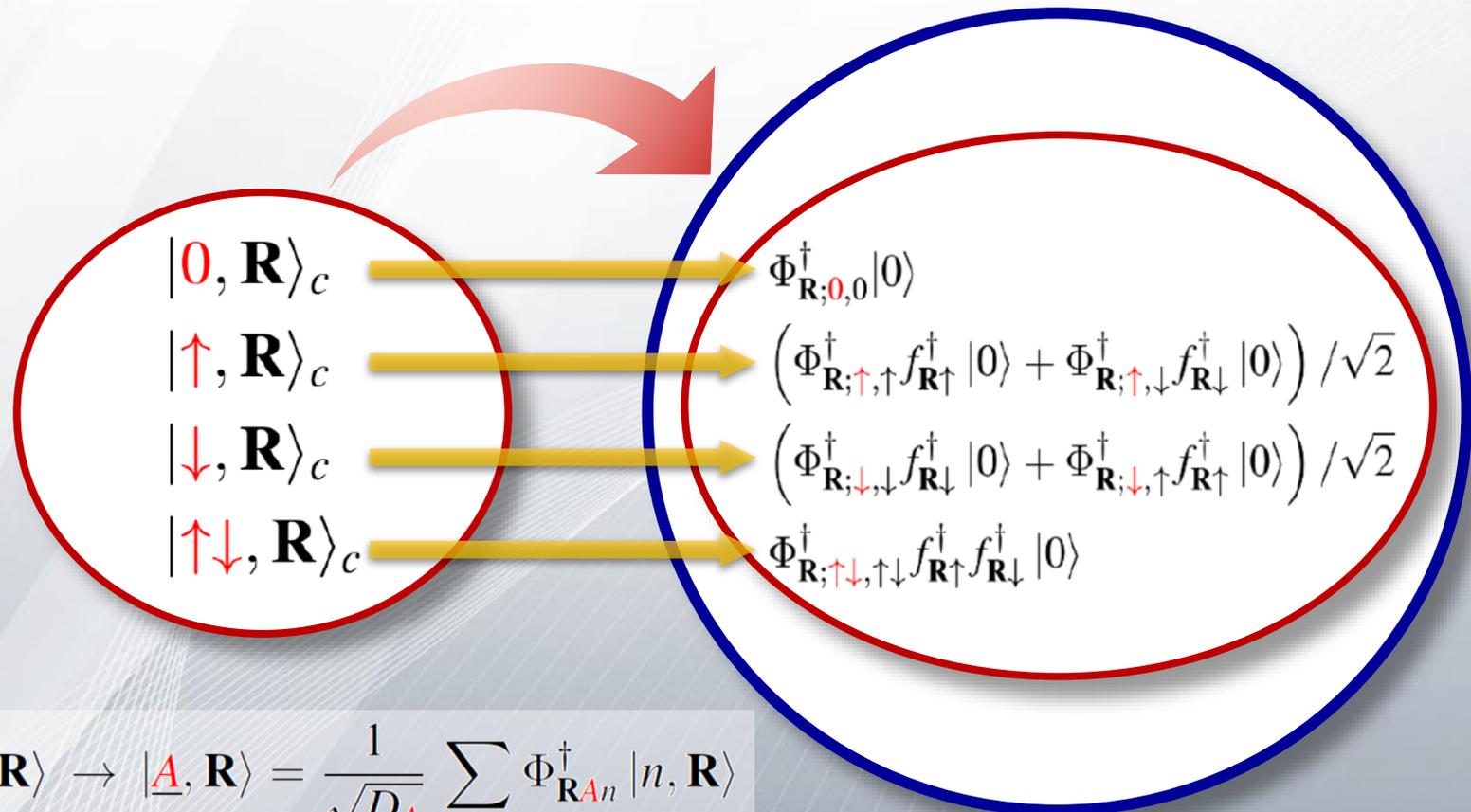


($\Phi_{\mathbf{R}A_n}$ only for $N_A = N_n$)

Quadratic part correlated local orbitals included in \mathcal{H}^{loc}

Slave-Boson Local Hilbert Space

$\mathcal{H}_{SB}^{\mathbf{R}}$ generated by “artificial” Bosonic and Fermionic degrees of freedom
 (dimension $\mathcal{H}_{SB}^{\mathbf{R}} = \infty$)



$$|A, \mathbf{R}\rangle \rightarrow |\underline{A}, \mathbf{R}\rangle = \frac{1}{\sqrt{D_A}} \sum_n \Phi_{\mathbf{R}A_n}^\dagger |n, \mathbf{R}\rangle$$

Gutzwiller constraints (introducing definition F_a matrices)

Operatorial Gutzwiller Constraints

Physical subspace $h_{SB}^{\mathbf{R}}$ of $\mathcal{H}_{SB}^{\mathbf{R}}$ identified by operatorial identities

$$\begin{aligned} & \Phi_{\mathbf{R};0,0}^\dagger |0\rangle \\ & \left(\Phi_{\mathbf{R};\uparrow,\uparrow}^\dagger f_{\mathbf{R}\uparrow}^\dagger |0\rangle + \Phi_{\mathbf{R};\uparrow,\downarrow}^\dagger f_{\mathbf{R}\downarrow}^\dagger |0\rangle \right) / \sqrt{2} \\ & \left(\Phi_{\mathbf{R};\downarrow,\downarrow}^\dagger f_{\mathbf{R}\downarrow}^\dagger |0\rangle + \Phi_{\mathbf{R};\downarrow,\uparrow}^\dagger f_{\mathbf{R}\uparrow}^\dagger |0\rangle \right) / \sqrt{2} \\ & \Phi_{\mathbf{R};\uparrow\downarrow,\uparrow\downarrow}^\dagger f_{\mathbf{R}\uparrow}^\dagger f_{\mathbf{R}\downarrow}^\dagger |0\rangle \quad h_{SB}^{\mathbf{R}} \end{aligned}$$

$\mathcal{H}_{SB}^{\mathbf{R}}$

$$\sum_{An} \Phi_{\mathbf{R}An}^\dagger \Phi_{\mathbf{R}An} = 1$$

$$\sum_{Ann} [F_a^\dagger F_b]_{mn} \Phi_{\mathbf{R}An}^\dagger \Phi_{\mathbf{R}Am} = f_{\mathbf{R}a}^\dagger f_{\mathbf{R}b}$$

$$\left([F_a]_{nm} \equiv \langle n, \mathbf{R} | f_{\mathbf{R}a} | m, \mathbf{R} \rangle \right)$$

$$|A, \mathbf{R}\rangle \rightarrow |\underline{A}, \mathbf{R}\rangle = \frac{1}{\sqrt{D_A}} \sum_n \Phi_{\mathbf{R}An}^\dagger |n, \mathbf{R}\rangle$$

Slave Bosons = “Local Modes” (interaction becomes *quadratic*)

The Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^{\dagger} c_{\mathbf{R}'\sigma} + \sum_{\mathbf{R}} U c_{\mathbf{R}\uparrow}^{\dagger} c_{\mathbf{R}\uparrow} c_{\mathbf{R}\downarrow}^{\dagger} c_{\mathbf{R}\downarrow}$$

SB representation local interaction

$$\hat{H}^{\text{loc}} \equiv \sum_{\mathbf{R}} U c_{\mathbf{R}\uparrow}^{\dagger} c_{\mathbf{R}\uparrow} c_{\mathbf{R}\downarrow}^{\dagger} c_{\mathbf{R}\downarrow} = \sum_{\mathbf{R}} \sum_{AB} [H^{\text{loc}}]_{AB} |A, \mathbf{R}\rangle \langle B, \mathbf{R}|$$

$$\underline{\hat{H}}^{\text{loc}} \equiv \sum_{\mathbf{R}} \sum_n U \Phi_{\mathbf{R};\uparrow\downarrow,n}^{\dagger} \Phi_{\mathbf{R};\uparrow\downarrow,n} = \sum_{\mathbf{R}} \sum_{AB} [H^{\text{loc}}]_{AB} \sum_n \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}Bn}$$

$\underline{\hat{H}}^{\text{loc}}$ is a faithful representation of \hat{H}^{loc} , i.e.:

$$\langle \underline{A}, \mathbf{R} | \underline{\hat{H}}^{\text{loc}} | \underline{B}, \mathbf{R} \rangle = \langle A, \mathbf{R} | \hat{H}^{\text{loc}} | B, \mathbf{R} \rangle = [H^{\text{loc}}]_{AB} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & U \end{bmatrix}_{AB}$$

The Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^{\dagger} c_{\mathbf{R}'\sigma} + \sum_{\mathbf{R}} U c_{\mathbf{R}\uparrow}^{\dagger} c_{\mathbf{R}\uparrow} c_{\mathbf{R}\downarrow}^{\dagger} c_{\mathbf{R}\downarrow}$$

SB representation hopping (non-local) term
We look for SB representation Ladder operators

We will construct Bosonic $\hat{\mathcal{R}}_{\mathbf{R}a\alpha}$ such that:

$$\underline{c}_{\mathbf{R}\alpha}^{\dagger} \equiv \sum_a \hat{\mathcal{R}}_{\mathbf{R}a\alpha} [\Phi_{\mathbf{R}An}, \Phi_{\mathbf{R}An}^{\dagger}] f_{\mathbf{R}a}^{\dagger}.$$

$$\langle \underline{A}, \mathbf{R} | \underline{c}_{\mathbf{R}\alpha}^{\dagger} | \underline{B}, \mathbf{R} \rangle = \langle A, \mathbf{R} | c_{\mathbf{R}\alpha}^{\dagger} | B, \mathbf{R} \rangle \quad \forall A, B$$

Choice of $\hat{\mathcal{R}}_{\mathbf{R}a\alpha}$ affects mean-field approximation

Construction of $\hat{\mathcal{R}}_{\mathbf{R}a\alpha}$ such that

$$\langle \underline{A}, \mathbf{R} | \underline{c}_{\mathbf{R}\alpha}^\dagger | \underline{B}, \mathbf{R} \rangle = \langle A, \mathbf{R} | c_{\mathbf{R}\alpha}^\dagger | B, \mathbf{R} \rangle \quad \forall A, B$$

**With no loss of generality,
 we can search for solution represented as:**

$$\begin{aligned} \hat{\mathcal{R}}_{\mathbf{R}a\alpha} = & : \left[r_{\mathbf{R}a\alpha}^{(0)} + [r_{\mathbf{R}a\alpha}^{(2)}]_{An,Bm} \Phi_{\mathbf{R}An}^\dagger \Phi_{\mathbf{R}Bm} + \right. \\ & \left. + [r_{\mathbf{R}a\alpha}^{(4)}]_{An,Bm,Cl,Dr} \Phi_{\mathbf{R}An}^\dagger \Phi_{\mathbf{R}Bm}^\dagger \Phi_{\mathbf{R}Cl} \Phi_{\mathbf{R}Dr} + \dots \right] : \end{aligned}$$

One of the possible solutions is (PRB 76, 155102 (2007)) :

$$\hat{\mathcal{R}}_{\mathbf{R}a\alpha} = \sum_{AB} \sum_{nm} \frac{1}{N_A} \sqrt{\frac{D_B}{D_A}} [F_{\alpha}^\dagger]_{AB} [F_a^\dagger]_{nm} \Phi_{\mathbf{R}An}^\dagger \Phi_{\mathbf{R}Bm}$$

Alternative $\hat{\mathcal{R}}_{\mathbf{R}a\alpha}$ suitable for MF approximation
 arXiv:1606.09614 (2016)

$$\hat{\mathcal{R}}_{\mathbf{R}a\alpha} \equiv \sum_{ABnmb} \frac{1}{N_A} \sqrt{\frac{D_B}{D_A}} [F_{\alpha}^{\dagger}]_{AB} [F_b^{\dagger}]_{nm}$$

$$: \Phi_{\mathbf{R}An}^{\dagger} \left[\hat{\mathbf{1}} + \left(N_A \sqrt{\frac{D_A}{D_B}} - 1 \right) \sum_{Cl} \Phi_{\mathbf{R}Cl}^{\dagger} \Phi_{\mathbf{R}Cl} \right]$$

$$\left[\left[\hat{\mathbf{1}} - \hat{\Delta}_p \right]^{[-\frac{1}{2}]} \bullet \left[\hat{\mathbf{1}} - \hat{\Delta}_h \right]^{[-\frac{1}{2}]} \right]_{\mathbf{R}ba} \Phi_{\mathbf{R}Bm} :$$

where:

$$[\hat{\Delta}_p]_{\mathbf{R}ab} \equiv \sum_{Anm} [F_a^{\dagger} F_b]_{mn} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}Am}$$

$$[\hat{\Delta}_h]_{\mathbf{R}ab} \equiv \sum_{Anm} [F_b F_a^{\dagger}]_{mn} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}Am}$$

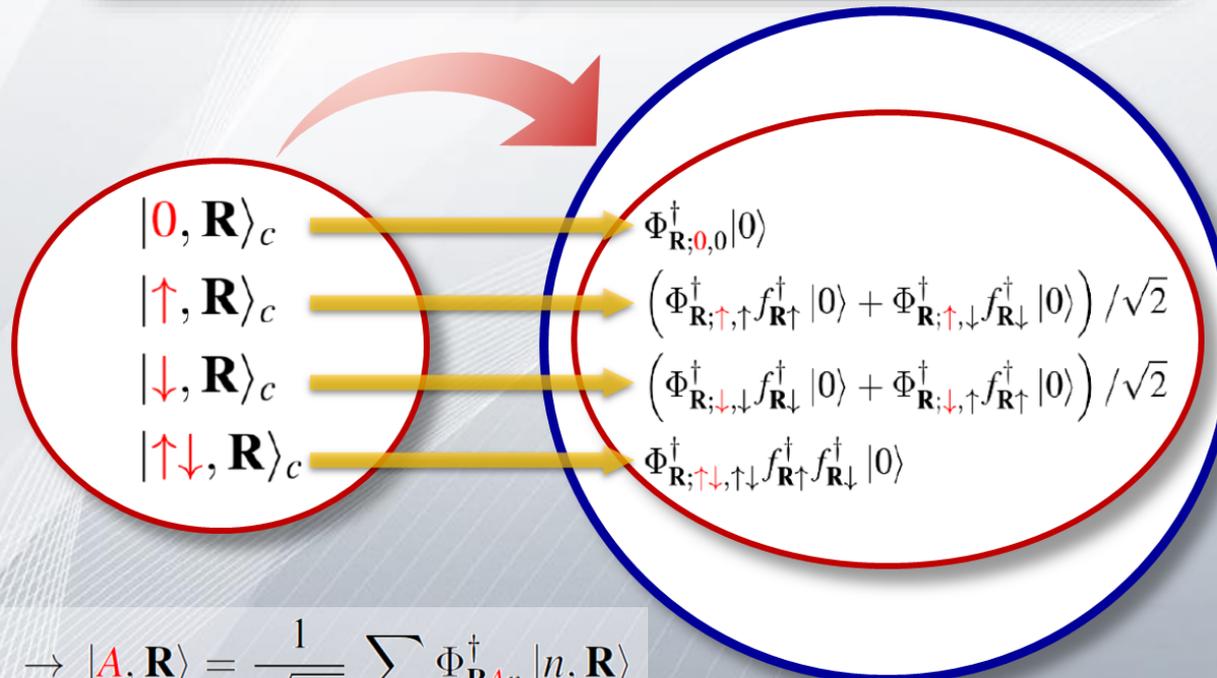
$$\left[\hat{\mathbf{1}} - \hat{\Delta} \right]^{[-\frac{1}{2}]} \equiv \sum_{r=0}^{\infty} (-1)^r \binom{\frac{1}{2}}{r} [\hat{\Delta}]^{[r]}$$

Summary SB reformulation: quadratic interaction, “renormalized” hopping

The Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^{\dagger} c_{\mathbf{R}'\sigma} + \sum_{\mathbf{R}} U c_{\mathbf{R}\uparrow}^{\dagger} c_{\mathbf{R}\uparrow} c_{\mathbf{R}\downarrow}^{\dagger} c_{\mathbf{R}\downarrow}$$

$$\underline{\hat{H}} = \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} \underline{c}_{\mathbf{R}\sigma}^{\dagger} \underline{c}_{\mathbf{R}'\sigma} + \sum_{\mathbf{R}} \sum_n U \Phi_{\mathbf{R};\uparrow\downarrow,n}^{\dagger} \Phi_{\mathbf{R};\uparrow\downarrow,n}$$



$$|A, \mathbf{R}\rangle \rightarrow |\underline{A}, \mathbf{R}\rangle = \frac{1}{\sqrt{D_A}} \sum_n \Phi_{\mathbf{R}A_n}^{\dagger} |n, \mathbf{R}\rangle$$

Mean Field theory as a variational approximation

The Slave Boson Hubbard Hamiltonian

$$\hat{H} = \sum_{RR'} \sum_{\sigma} \epsilon_{RR'} c_{R\sigma}^{\dagger} c_{R'\sigma} + \sum_{\mathbf{R}} \sum_n U \Phi_{\mathbf{R};\uparrow\downarrow,n}^{\dagger} \Phi_{\mathbf{R};\uparrow\downarrow,n}$$

$$\mathcal{H}_{SB}^{\mathbf{R}} = \Phi_{\mathbf{R};0,0}^{\dagger} |0\rangle + \left(\Phi_{\mathbf{R};\uparrow,\uparrow}^{\dagger} f_{\mathbf{R}\uparrow}^{\dagger} |0\rangle + \Phi_{\mathbf{R};\uparrow,\downarrow}^{\dagger} f_{\mathbf{R}\downarrow}^{\dagger} |0\rangle \right) / \sqrt{2} + \left(\Phi_{\mathbf{R};\downarrow,\downarrow}^{\dagger} f_{\mathbf{R}\downarrow}^{\dagger} |0\rangle + \Phi_{\mathbf{R};\downarrow,\uparrow}^{\dagger} f_{\mathbf{R}\uparrow}^{\dagger} |0\rangle \right) / \sqrt{2} + \Phi_{\mathbf{R};\uparrow\downarrow,\uparrow\downarrow}^{\dagger} f_{\mathbf{R}\uparrow}^{\dagger} f_{\mathbf{R}\downarrow}^{\dagger} |0\rangle$$

$h_{SB}^{\mathbf{R}}$

$$\sum_{An} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}An} = 1$$

$$\sum_{Anm} [F_a^{\dagger} F_b]_{mn} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}Am} = f_{\mathbf{R}a}^{\dagger} f_{\mathbf{R}b}$$

$$c_{\mathbf{R}\alpha}^{\dagger} \equiv \sum_a \hat{\mathcal{R}}_{\mathbf{R}\alpha a} [\Phi_{\mathbf{R}An}, \Phi_{\mathbf{R}An}^{\dagger}] f_{\mathbf{R}a}^{\dagger}$$

Assuming following variational ansatz:

$$|\Psi_{SB}\rangle = |\Psi_0\rangle \otimes |\phi\rangle, \quad (\Phi_{\mathbf{R}An} |\phi\rangle = \phi_{An} |\phi\rangle)$$

We need to calculate average: 1) interaction, 2) constraints, 3) hopping

The Slave Boson Hubbard Hamiltonian

$$\hat{H} = \sum_{RR'} \sum_{\sigma} \epsilon_{RR'} c_{R\sigma}^{\dagger} c_{R'\sigma} + \sum_{R} \sum_n U \Phi_{R;\uparrow\downarrow,n}^{\dagger} \Phi_{R;\uparrow\downarrow,n}$$

$$\mathcal{H}_{SB}^R = \Phi_{R;0,0}^{\dagger} |0\rangle + \frac{1}{\sqrt{2}} (\Phi_{R;\uparrow,\uparrow}^{\dagger} f_{R\uparrow}^{\dagger} |0\rangle + \Phi_{R;\uparrow,\downarrow}^{\dagger} f_{R\downarrow}^{\dagger} |0\rangle) + \frac{1}{\sqrt{2}} (\Phi_{R;\downarrow,\downarrow}^{\dagger} f_{R\downarrow}^{\dagger} |0\rangle + \Phi_{R;\downarrow,\uparrow}^{\dagger} f_{R\uparrow}^{\dagger} |0\rangle) + \Phi_{R;\uparrow\downarrow,\uparrow\downarrow}^{\dagger} f_{R\uparrow}^{\dagger} f_{R\downarrow}^{\dagger} |0\rangle$$

h_{SB}^R

$$\langle \Psi_{SB} | \sum_{An} \Phi_{RAn}^{\dagger} \Phi_{RAn} - \hat{1} | \Psi_{SB} \rangle = 0$$

$$\langle \Psi_{SB} | \sum_{Anm} [F_a^{\dagger} F_b]_{mn} \Phi_{RAn}^{\dagger} \Phi_{RAm} - f_{Ra}^{\dagger} f_{Rb} | \Psi_{SB} \rangle = 0$$

$$c_{R\alpha}^{\dagger} \equiv \sum_a \hat{\mathcal{R}}_{Ra\alpha} [\Phi_{RAn}, \Phi_{RAn}^{\dagger}] f_{Ra}^{\dagger}$$

Assuming following variational ansatz:

$$|\Psi_{SB}\rangle = |\Psi_0\rangle \otimes |\phi\rangle, \quad \text{Constrained Minimization}$$

Expectation value Local Interaction ($\phi\phi^\dagger$ local reduced density matrix)

The Slave Boson Hubbard Hamiltonian

$$\hat{H} = \sum_{RR'} \sum_{\sigma} \epsilon_{RR'} c_{R\sigma}^\dagger c_{R'\sigma} + \sum_{\mathbf{R}} \sum_n U \Phi_{\mathbf{R};\uparrow\downarrow,n}^\dagger \Phi_{\mathbf{R};\uparrow\downarrow,n}$$

Assuming following variational ansatz:

$$|\Psi_{\text{SB}}\rangle = |\Psi_0\rangle \otimes |\phi\rangle$$

Local interaction:

$$\langle \phi | \sum_{\mathbf{R}} \sum_n U \Phi_{\mathbf{R};\uparrow\downarrow,n}^\dagger \Phi_{\mathbf{R};\uparrow\downarrow,n} | \phi \rangle = \text{Tr}[\phi\phi^\dagger H^{\text{loc}}]$$

$$\left(H_{AB}^{\text{loc}} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & U \end{bmatrix}_{AB} \right)$$

Expectation value Gutzwiller Constraints

The Slave Boson Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^{\dagger} c_{\mathbf{R}'\sigma} + \sum_{\mathbf{R}} \sum_n U \Phi_{\mathbf{R};\uparrow\downarrow,n}^{\dagger} \Phi_{\mathbf{R};\uparrow\downarrow,n}$$

Assuming following variational ansatz:

$$|\Psi_{\text{SB}}\rangle = |\Psi_0\rangle \otimes |\phi\rangle$$

Gutzwiller constraints:

$$\langle \Psi_{\text{SB}} | \sum_{An} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}An} - \hat{1} | \Psi_{\text{SB}} \rangle = \text{Tr}[\phi^{\dagger} \phi] - 1 = 0$$

$$\langle \Psi_{\text{SB}} | \sum_{Ann} [F_a^{\dagger} F_b]_{mn} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}Am} - f_{\mathbf{R}a}^{\dagger} f_{\mathbf{R}b} | \Psi_{\text{SB}} \rangle = \text{Tr}[\phi^{\dagger} \phi F_a^{\dagger} F_b] - \langle \Psi_0 | f_{\mathbf{R}a}^{\dagger} f_{\mathbf{R}b} | \Psi_0 \rangle = 0$$

Expectation value Renormalization Operators

The Slave Boson Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^{\dagger} c_{\mathbf{R}'\sigma} + \sum_{\mathbf{R}} \sum_n U \Phi_{\mathbf{R};\uparrow\downarrow,n}^{\dagger} \Phi_{\mathbf{R};\uparrow\downarrow,n}$$

Assuming following variational ansatz:

$$|\Psi_{\text{SB}}\rangle = |\Psi_0\rangle \otimes |\phi\rangle$$

Renormalization factors:

$$\langle \phi | c_{\mathbf{R}\alpha}^{\dagger} | \phi \rangle = \sum_a \langle \phi | \hat{\mathcal{R}}_{\mathbf{R}a\alpha} [\Phi_{\mathbf{R}An}, \Phi_{\mathbf{R}An}^{\dagger}] | \phi \rangle f_{\mathbf{R}a}^{\dagger} \equiv \sum_a \mathcal{R}_{a\alpha} [\phi_{An}, \phi_{An}^{\dagger}] f_{\mathbf{R}a}^{\dagger}$$

Alternative $\hat{\mathcal{R}}_{\mathbf{R}a\alpha}$ suitable for MF approximation

$$\hat{\mathcal{R}}_{\mathbf{R}a\alpha} \equiv \sum_{ABnmb} \frac{1}{N_A} \sqrt{\frac{D_B}{D_A}} [F_{\alpha}^{\dagger}]_{AB} [F_b^{\dagger}]_{nm}$$

$$: \Phi_{\mathbf{R}An}^{\dagger} \left[\hat{\mathbf{1}} + \left(N_A \sqrt{\frac{D_A}{D_B}} - 1 \right) \sum_{cl} \Phi_{\mathbf{R}Cl}^{\dagger} \Phi_{\mathbf{R}Cl} \right]$$

$$\left[\left[\hat{\mathbf{1}} - \hat{\Delta}_p \right]^{[-\frac{1}{2}]} \bullet \left[\hat{\mathbf{1}} - \hat{\Delta}_h \right]^{[-\frac{1}{2}]} \right]_{\mathbf{R}ba} \Phi_{\mathbf{R}Bm} :$$

where:

$$[\hat{\Delta}_p]_{\mathbf{R}ab} \equiv \sum_{Anm} [F_a^{\dagger} F_b]_{mn} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}Am}$$

$$[\hat{\Delta}_h]_{\mathbf{R}ab} \equiv \sum_{Anm} [F_b F_a^{\dagger}]_{mn} \Phi_{\mathbf{R}An}^{\dagger} \Phi_{\mathbf{R}Am}$$

$$\left[\hat{\mathbf{1}} - \hat{\Delta} \right]^{[-\frac{1}{2}]} \equiv \sum_{r=0}^{\infty} (-1)^r \binom{\frac{1}{2}}{r} [\hat{\Delta}]^{[r]}$$

Mean Field renormalization factors

$$\mathcal{R}_{a\alpha} \equiv \langle \phi | \hat{\mathcal{R}}_{\mathbf{R}a\alpha} | \phi \rangle = \sum_b \text{Tr}[\phi^\dagger F_\alpha^\dagger \phi F_b] [(1 - \Delta_p) \Delta_p]_{ba}^{-\frac{1}{2}}$$

where: $[\Delta_p]_{ab} = \text{Tr}[\phi^\dagger \phi F_a^\dagger F_b]$

Consequently, in summary:

$$\langle \Psi_{SB} | \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^\dagger c_{\mathbf{R}'\sigma} | \Psi_{SB} \rangle = |\mathcal{R}(\phi)|^2 \langle \Psi_0 | \sum_{\mathbf{R}\mathbf{R}'} \sum_{\sigma} \epsilon_{\mathbf{R}\mathbf{R}'} f_{\mathbf{R}\sigma}^\dagger f_{\mathbf{R}'\sigma} | \Psi_0 \rangle$$

$$\langle \Psi_{SB} | \sum_{\mathbf{R}n} U \Phi_{\mathbf{R};\uparrow\downarrow,n}^\dagger \Phi_{\mathbf{R};\uparrow\downarrow,n} | \Psi_{SB} \rangle = \text{Tr}[\phi \phi^\dagger H^{\text{loc}}]$$

$$\langle \Psi_{SB} | \sum_{An} \Phi_{\mathbf{R}An}^\dagger \Phi_{\mathbf{R}An} - \hat{1} | \Psi_{SB} \rangle = \text{Tr}[\phi^\dagger \phi] - 1 = 0$$

$$\langle \Psi_{SB} | \sum_{Ann} [F_a^\dagger F_b]_{mn} \Phi_{\mathbf{R}An}^\dagger \Phi_{\mathbf{R}Am} - f_{\mathbf{R}a}^\dagger f_{\mathbf{R}b} | \Psi_{SB} \rangle = \text{Tr}[\phi^\dagger \phi F_a^\dagger F_b] - \langle \Psi_0 | f_{\mathbf{R}a}^\dagger f_{\mathbf{R}b} | \Psi_0 \rangle = 0$$

Observation: number of independent SB amplitudes (ignoring symmetry)

Number of independent complex parameters ϕ is
 $2^2 \times 2^2$

(as dimension “impurity model” whose bath has same dimension of the “impurity” $\mathcal{H}_F^{\mathbf{R}}$)

$$|A\rangle = [\hat{c}_1^\dagger]^{n_1} \cdots [\hat{c}_M^\dagger]^{n_M} |0\rangle$$

Impurity

$$|n\rangle = [\hat{f}_1^\dagger]^{n_1} \cdots [\hat{f}_M^\dagger]^{n_M} |0\rangle$$

Bath

Quadratic part correlated local orbitals included in \mathcal{H}^{loc}

Generic Hubbard Hamiltonian

$$\hat{H} = \sum_{\mathbf{k}} \sum_{ij} \sum_{\alpha\beta} \epsilon_{\mathbf{k},ij}^{\alpha\beta} c_{\mathbf{k}i\alpha}^\dagger c_{\mathbf{k}j\beta} + \sum_{\mathbf{R}i \in \text{corr}} \hat{H}_i^{\text{loc}} [\{c_{\mathbf{R}i\alpha}^\dagger\}, \{c_{\mathbf{R}i\alpha}\}]$$

$$\epsilon_{\mathbf{k}} = \begin{bmatrix} i=0 & * & * \\ * & i=1 & * \\ * & * & i=2 \end{bmatrix}$$

\mathbf{R} = label unit cell

\mathbf{k} = Fourier-conjugate of \mathbf{R}

$$\sum_{\mathbf{k}} \epsilon_{\mathbf{k},ii} = 0 \quad \forall i \text{ correlated}$$

α, β = orbitals in \mathbf{R}, i

(Example: $i = 0$: uncorrelated orbitals; $i = 1$: d orbitals atom 1
 $i = 2$: f orbitals atom 2 ...)

Constrained minimization problem, $2^{M_i} \times 2^{M_i}$ independent SB amplitudes

The variational energy

$$\hat{H} = \sum_{\mathbf{k}} \sum_{\alpha\beta} \boxed{\epsilon_{\mathbf{k},ij}^{\alpha\beta}} c_{\mathbf{k}i\alpha}^\dagger c_{\mathbf{k}j\beta} + \sum_{\mathbf{R}i} \boxed{\hat{H}_{\mathbf{R}i}^{\text{loc}} [\{\hat{c}_{\mathbf{R}i\alpha}^\dagger\}, \{\hat{c}_{\mathbf{R}i\alpha}\}]}$$

$$\mathcal{E}[\Psi_0, \{\phi_i\}] = \frac{1}{\mathcal{N}} \sum_{\mathbf{k},ij} \sum_{ab} \left[\mathcal{R}_i \epsilon_{\mathbf{k},ij} \mathcal{R}_j^\dagger \right]_{ab} \langle \Psi_0 | f_{\mathbf{k}i\alpha}^\dagger f_{\mathbf{k}j\beta} | \Psi_0 \rangle$$

$$+ \sum_{i \in \text{corr}} \text{Tr} \left[\phi_i \phi_i^\dagger H_i^{\text{loc}} \right]$$

where

$$[\mathcal{R}_i]_{a\alpha} = \sum_b \text{Tr} \left[\phi_i^\dagger F_{i\alpha}^\dagger \phi_i F_{ib} \right] [\Delta_{pi}(1 - \Delta_{pi})]_{ba}^{-\frac{1}{2}}$$

to be minimized satisfying the Gutzwiller constraints:

$$\text{Tr} \left[\phi_i^\dagger \phi_i \right] = \langle \Psi_0 | \Psi_0 \rangle = 1$$

$$\text{Tr} \left[\phi_i^\dagger \phi_i F_{i\alpha}^\dagger F_{ib} \right] = \langle \Psi_0 | f_{\mathbf{R}i\alpha}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle \equiv \Delta_{pi}$$

Step 1: promoting Δ_p , \mathcal{R} to independent variables using Lagrange multipliers

Functional formulation SB

$$\begin{aligned} \mathcal{L}[\Psi_0, E; \phi, E^c; \mathcal{R}, \mathcal{R}^\dagger, \lambda; \mathcal{D}, \mathcal{D}^\dagger, \lambda^c; \Delta_p] = & \\ \frac{1}{\mathcal{N}} \langle \Psi_0 | \hat{H}_G^{\text{qp}}[\mathcal{R}, \mathcal{R}^\dagger; \lambda] | \Psi_0 \rangle + E(1 - \langle \Psi_0 | \Psi_0 \rangle) + & \\ \sum_i \text{Tr} \left[\phi_i \phi_i^\dagger H_i^{\text{loc}} + \sum_{a\alpha} \left([\mathcal{D}i]_{a\alpha} \phi_i^\dagger F_{i\alpha}^\dagger \phi_i F_{ia} + \text{H.c.} \right) + \sum_{ab} [\lambda_i^c]_{ab} \phi_i^\dagger \phi_i F_{ia}^\dagger F_{ib} \right] + & \\ \sum_i E_i^c \left(1 - \text{Tr} \left[\phi_i^\dagger \phi_i \right] \right) & \\ - \sum_i \left[\sum_{ab} \left([\lambda_i]_{ab} + [\lambda_i^c]_{ab} \right) [\Delta_{pi}]_{ab} + \sum_{c\alpha} \left([\mathcal{D}i]_{a\alpha} [\mathcal{R}i]_{c\alpha} [\Delta_{pi}(1 - \Delta_{pi})]_{c\alpha}^{\frac{1}{2}} + \text{c.c.} \right) \right] & \end{aligned}$$

where

$$\hat{H}_G^{\text{qp}}[\mathcal{R}, \mathcal{R}^\dagger; \lambda] \equiv \sum_{k,ij} \sum_{ab} \left[\mathcal{R}_i \epsilon_{k,ij} \mathcal{R}_j^\dagger \right]_{ab} f_{kia}^\dagger f_{kjb} + \sum_{Ri,ab} [\lambda_i]_{ab} f_{Ria}^\dagger f_{Rib}$$

Now quadratic functional of ϕ (linear in ϕ and ϕ^\dagger)!
 ($\frac{\delta \mathcal{L}}{\delta \phi} = 0$ same complexity of ground-state eigenvalue problem ...)

Step 2: Eliminating (formally) $|\Psi_0\rangle$ and E

Functional formulation SB

$$\mathcal{L}[\Psi_0, E; \phi, E^c; \mathcal{R}, \mathcal{R}^\dagger, \lambda; \mathcal{D}, \mathcal{D}^\dagger, \lambda^c; \Delta_p] =$$

$$\frac{1}{\mathcal{N}} \langle \Psi_0 | \hat{H}_G^{\text{qp}}[\mathcal{R}, \mathcal{R}^\dagger; \lambda] | \Psi_0 \rangle + E(1 - \langle \Psi_0 | \Psi_0 \rangle) +$$

$$\sum_i \text{Tr} \left[\phi_i \phi_i^\dagger H_i^{\text{loc}} + \sum_{a\alpha} \left([\mathcal{D}_i]_{a\alpha} \phi_i^\dagger F_{i\alpha}^\dagger \phi_i F_{ia} + \text{H.c.} \right) + \sum_{ab} [\lambda_i^c]_{ab} \phi_i^\dagger \phi_i F_{ia}^\dagger F_{ib} \right] +$$

$$\sum_i E_i^c \left(1 - \text{Tr} \left[\phi_i^\dagger \phi_i \right] \right)$$

$$- \sum_i \left[\sum_{ab} \left([\lambda_i]_{ab} + [\lambda_i^c]_{ab} \right) [\Delta_{pi}]_{ab} + \sum_{ca\alpha} \left([\mathcal{D}_i]_{a\alpha} [\mathcal{R}_i]_{c\alpha} [\Delta_{pi}(1 - \Delta_{pi})]_{c\alpha}^{\frac{1}{2}} + \text{c.c.} \right) \right]$$

where

$$\hat{H}_G^{\text{qp}}[\mathcal{R}, \mathcal{R}^\dagger; \lambda] \equiv \sum_{k,ij} \sum_{ab} \left[\mathcal{R}_i \epsilon_{k,ij} \mathcal{R}_j^\dagger \right]_{ab} f_{kia}^\dagger f_{kjb} + \sum_{Ri,ab} [\lambda_i]_{ab} f_{Ria}^\dagger f_{Rib}$$

Step 2: Eliminating (formally) $|\Psi_0\rangle$ and E

Functional formulation SB

$$\mathcal{L}[\phi, E^c; \mathcal{R}, \mathcal{R}^\dagger, \lambda; \mathcal{D}, \mathcal{D}^\dagger, \lambda^c; \Delta_p] =$$

$$\frac{\mathcal{T}}{\mathcal{N}} \sum_{k, \omega} \text{Tr} \log \left(\frac{1}{i\omega - \mathcal{R} \epsilon_k \mathcal{R}^\dagger - \lambda} \right) e^{i\omega 0^+} +$$

$$\sum_i \text{Tr} \left[\phi_i \phi_i^\dagger H_i^{\text{loc}} + \sum_{a\alpha} \left([\mathcal{D}_i]_{a\alpha} \phi_i^\dagger F_{i\alpha}^\dagger \phi_i F_{ia} + \text{H.c.} \right) + \sum_{ab} [\lambda_i^c]_{ab} \phi_i^\dagger \phi_i F_{ia}^\dagger F_{ib} \right] +$$

$$\sum_i E_i^c \left(1 - \text{Tr} \left[\phi_i^\dagger \phi_i \right] \right)$$

$$- \sum_i \left[\sum_{ab} \left([\lambda_i]_{ab} + [\lambda_i^c]_{ab} \right) [\Delta_{pi}]_{ab} + \sum_{ca\alpha} \left([\mathcal{D}_i]_{a\alpha} [\mathcal{R}_i]_{c\alpha} [\Delta_{pi}(1 - \Delta_{pi})]_{c\alpha}^{\frac{1}{2}} + \text{c.c.} \right) \right]$$

where

$$\epsilon_k = \begin{bmatrix} i=0 & * & * \\ * & i=1 & * \\ * & * & i=2 \end{bmatrix}; \quad \mathcal{R} = \begin{bmatrix} \mathbb{1} & 0 & 0 \\ 0 & \mathcal{R}_{i=1} & 0 \\ 0 & 0 & \mathcal{R}_{i=2} \end{bmatrix}; \quad \lambda = \begin{bmatrix} 0 & 0 & 0 \\ 0 & \lambda_{i=1} & 0 \\ 0 & 0 & \lambda_{i=2} \end{bmatrix}$$

Step 3: Re-interpretation ϕ_i using Schmidt decomposition

Functional formulation SB

$$\mathcal{L}[\phi, E^c; \mathcal{R}, \mathcal{R}^\dagger, \lambda; \mathcal{D}, \mathcal{D}^\dagger, \lambda^c; \Delta_p] = \frac{\mathcal{T}}{\mathcal{N}} \sum_{k, \omega} \text{Tr} \log \left(\frac{1}{i\omega - \mathcal{R} \epsilon_k \mathcal{R}^\dagger - \lambda} \right) e^{i\omega 0^+} +$$

$$\sum_i \text{Tr} \left[\phi_i \phi_i^\dagger H_i^{\text{loc}} + \sum_{a\alpha} \left([\mathcal{D}_i]_{a\alpha} \phi_i^\dagger F_{i\alpha}^\dagger \phi_i F_{ia} + \text{H.c.} \right) + \sum_{ab} [\lambda_i^c]_{ab} \phi_i^\dagger \phi_i F_{ia}^\dagger F_{ib} \right] +$$

$$\sum_i E_i^c \left(1 - \text{Tr} [\phi_i^\dagger \phi_i] \right)$$

$$- \sum_i \left[\sum_{ab} \left([\lambda_i]_{ab} + [\lambda_i^c]_{ab} \right) [\Delta_{pi}]_{ab} + \sum_{c\alpha} \left([\mathcal{D}_i]_{a\alpha} [\mathcal{R}_i]_{c\alpha} [\Delta_{pi}(1 - \Delta_{pi})]_{c\alpha}^{\frac{1}{2}} + \text{c.c.} \right) \right]$$

Elements ϕ_i can be viewed as coefficients Schmidt decomposition:

$$|\Phi_i\rangle \equiv \sum_{An} e^{i\frac{\pi}{2} N_n(N_n-1)} [\phi_i]_{An} |A, i\rangle U_{\text{PH}} |n, i\rangle$$

$$|A\rangle = [\hat{c}_1^\dagger]^{n_1} \dots [\hat{c}_M^\dagger]^{n_M} |0\rangle \quad |n\rangle = [\hat{f}_1^\dagger]^{n_1} \dots [\hat{f}_M^\dagger]^{n_M} |0\rangle$$

Impurity

Bath

Step 3: Re-interpretation ϕ_i using Schmidt decomposition

Functional formulation SB

$$\mathcal{L}[\Phi, E^c; \mathcal{R}, \mathcal{R}^\dagger, \lambda; \mathcal{D}, \mathcal{D}^\dagger, \lambda^c; \Delta_p] = \frac{\mathcal{T}}{\mathcal{N}} \sum_{k, \omega} \text{Tr} \log \left(\frac{1}{i\omega - \mathcal{R}\epsilon_k \mathcal{R}^\dagger - \lambda} \right) e^{i\omega 0^+} +$$

$$\sum_i \left[\langle \Phi_i | \mathcal{H}_i^{\text{emb}}[\mathcal{D}_i, \mathcal{D}_i^\dagger; \lambda_i^c] | \Phi_i \rangle + E_i^c (1 - \langle \Phi_i | \Phi_i \rangle) \right]$$

$$- \sum_i \left[\sum_{ab} \left([\lambda_i]_{ab} + [\lambda_i^c]_{ab} \right) [\Delta_{pi}]_{ab} + \sum_{ca\alpha} \left([\mathcal{D}_i]_{a\alpha} [\mathcal{R}_i]_{c\alpha} [\Delta_{pi}(1 - \Delta_{pi})]_{c\alpha}^{\frac{1}{2}} + \text{c.c.} \right) \right]$$

where

$$\begin{aligned} \mathcal{H}_i^{\text{emb}}[\mathcal{D}_i, \mathcal{D}_i^\dagger; \lambda_i^c] &\equiv \hat{H}_i^{\text{loc}}[\{\hat{c}_{i\alpha}^\dagger\}, \{\hat{c}_{i\alpha}\}] \\ &+ \sum_{a\alpha} \left([\mathcal{D}_i]_{a\alpha} \hat{c}_{i\alpha}^\dagger \hat{f}_{ia} + \text{H.c.} \right) + \sum_{ab} [\lambda_i^c]_{ab} \hat{f}_{ib} \hat{f}_{ia}^\dagger \end{aligned}$$

Stationarity equations: $\lambda, \mathcal{R}, \Delta_p; \langle \Phi | \mathcal{E}^c; \mathbf{D}, \lambda^c$

SB stationarity equations

$$(\mathcal{R}, \lambda) \longrightarrow \frac{1}{\mathcal{N}} \left[\sum_k \Pi_i f \left(\mathcal{R} \epsilon_k \mathcal{R}^\dagger + \lambda \right) \Pi_i \right]_{ba} = [\Delta_{pi}]_{ab} \quad (1)$$

$$\frac{1}{\mathcal{N}} \left[\frac{1}{\mathcal{R}_i} \sum_k \Pi_i \mathcal{R} \epsilon_k \mathcal{R}^\dagger f \left(\mathcal{R} \epsilon_k \mathcal{R}^\dagger + \lambda \right) \Pi_i \right]_{\alpha a} = \sum_c [\mathcal{D}_i]_{c\alpha} [\Delta_{ip} (1 - \Delta_{ip})]_{ac}^{\frac{1}{2}} \quad (2)$$

$$\left[\sum_{cb\alpha} \frac{\partial}{\partial d_{is}^p} [\Delta_{pi} (1 - \Delta_{pi})]_{cb}^{\frac{1}{2}} [\mathcal{D}_i]_{b\alpha} [\mathcal{R}_i]_{c\alpha} + \text{c.c.} \right] + [l + l^c]_{is} = 0 \quad (3)$$

$$\mathcal{H}_i^{\text{emb}}[\mathcal{D}_i, \mathcal{D}_i^\dagger; \lambda_i^c] |\Phi_i\rangle = E_i^c |\Phi_i\rangle \quad (4)$$

$$[\mathcal{F}_i^{(1)}]_{\alpha a} \equiv \langle \Phi_i | \hat{c}_{i\alpha}^\dagger \hat{f}_{ia} | \Phi_i \rangle - \sum_c [\Delta_{ip} (1 - \Delta_{ip})]_{ca}^{\frac{1}{2}} [\mathcal{R}_i]_{c\alpha} = 0 \quad (5)$$

$$[\mathcal{F}_i^{(2)}]_{ab} \equiv \langle \Phi_i | \hat{f}_{ib} \hat{f}_{ia}^\dagger | \Phi_i \rangle - [\Delta_{pi}]_{ab} = 0 \quad (6)$$

where

$$\Delta_{pi} = \sum_s d_{is}^p {}^t h_{is}; \quad \lambda_i^c = \sum_s l_{is}^c h_{is}; \quad \lambda_i = \sum_s l_{is} h_{is}; \quad \mathcal{R}_i = \sum_s r_{is} h_{is}$$

“Adding interaction” to KS (only for selected correlated orbitals)

The Projector: Definition of the Correlated Orbitals

$$\hat{\Xi}(\mathbf{r}, \sigma) = \sum_{\sigma'} \sum_{ki, \pi \in P} \xi_{ki, \pi}(\mathbf{r}) \chi_{\sigma'}(\sigma) c_{ki\pi\sigma} + \hat{\Xi}_Q(\mathbf{r}, \sigma) \equiv \sum_i \hat{\Xi}_{P_i}(\mathbf{r}, \sigma) + \hat{\Xi}_Q(\mathbf{r}, \sigma)$$

$$\hat{A} = \sum_{\sigma} \int d\mathbf{r} \hat{\Xi}^{\dagger}(\mathbf{r}, \sigma) A \hat{\Xi}(\mathbf{r}, \sigma) \equiv \sum_i \hat{A}_i^{\text{loc}} + \hat{A}^{\text{hop}}$$

where

$$\hat{A}_i^{\text{loc}} \equiv \sum_{\sigma} \int d\mathbf{r} \hat{\Xi}_{P_i}^{\dagger}(\mathbf{r}, \sigma) A \hat{\Xi}_{P_i}(\mathbf{r}, \sigma); \quad \hat{A}^{\text{hop}} \equiv \hat{A} - \sum_i \hat{A}_i^{\text{loc}}.$$

$$A = \begin{bmatrix} A^{\text{hop}} & A^{\text{hop}} & A^{\text{hop}} \\ A^{\text{hop}} & A_{i=1}^{\text{loc}} & A^{\text{hop}} \\ A^{\text{hop}} & A^{\text{hop}} & A_{i=2}^{\text{loc}} \end{bmatrix}$$

LDA+SB as solving iteratively Kohn-Sham-Hubbard Hamiltonian

Functional formulation LDA+SB for non-linear double-counting

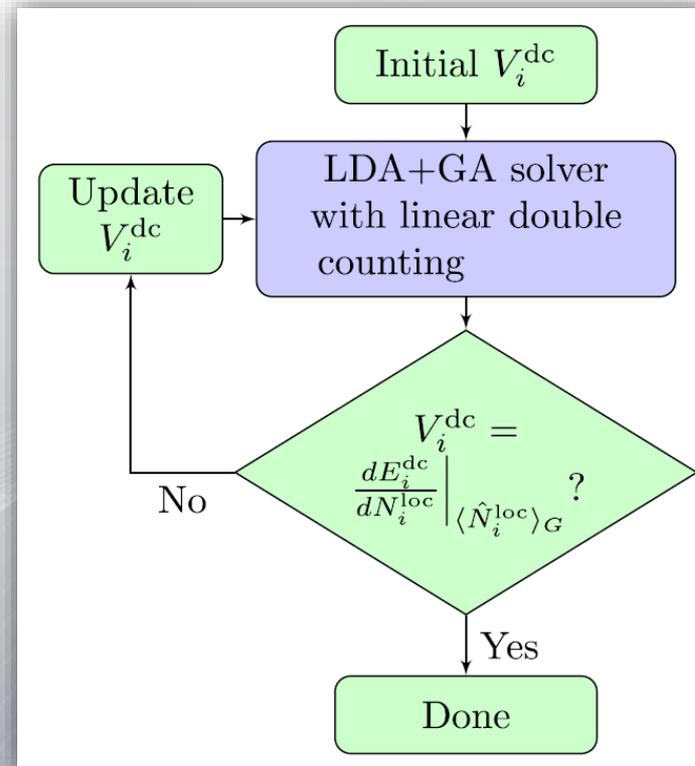
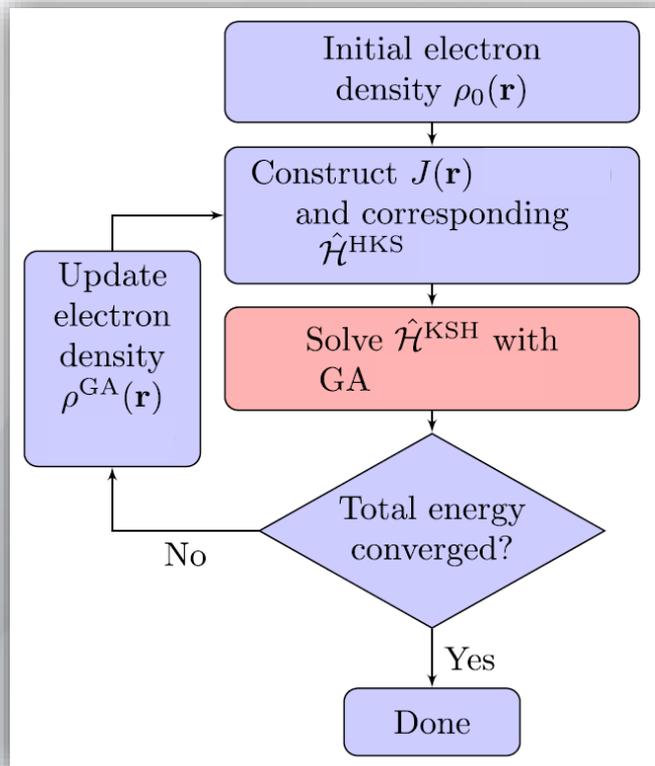
$$\begin{aligned} \Omega_{E^{\text{dc}}, N} [N^{\text{loc}}, V^{\text{dc}}; \rho(\mathbf{r}), J(\mathbf{r}); \Phi, E^c, \mathcal{R}, \mathcal{R}^\dagger, \lambda, \mu, \mathcal{D}, \mathcal{D}^\dagger, \lambda^c, \Delta_p] = \\ \mathcal{L}_{\text{KSH}} [J(\mathbf{r}); \phi, E^c; \mathcal{R}, \mathcal{R}^\dagger, \lambda; \mathcal{D}, \mathcal{D}^\dagger, \lambda^c; \Delta_p, \mu] + \\ \int d\mathbf{r} J(\mathbf{r}) \rho(\mathbf{r}) + E_{\text{Hxc}}^{\text{LDA}} [\rho(\mathbf{r})] + E_{\text{ion}} [\rho(\mathbf{r})] + E_{\text{ion-ion}} \\ + \sum_i [E_i^{\text{dc}} [N_i^{\text{loc}}] - V_i^{\text{dc}} N_i^{\text{loc}}] \end{aligned}$$

where \mathcal{L}_{KSH} is the SB functional of:

$$\hat{H}_{V^{\text{dc}}}^{\text{KSH}} [J(\mathbf{r})] \equiv -\hat{\Delta} + \frac{\delta E_{\text{Hxc}}^{\text{LDA}}}{\delta \rho(\mathbf{r})} + \frac{\delta E_{\text{ion}}}{\delta \rho(\mathbf{r})} + \sum_i \hat{H}_i^{\text{int}} - \sum_i V_i^{\text{dc}} \hat{N}_i^{\text{loc}}$$

LDA+SB as solving iteratively Kohn-Sham-Hubbard Hamiltonian

Functional formulation LDA+SB for non-linear double-counting



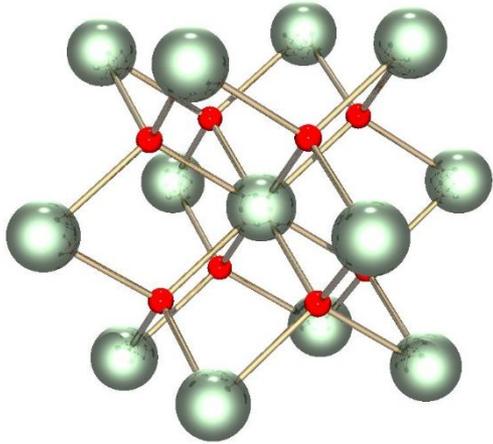
$$\hat{H}_{V^{\text{dc}}}^{\text{KSH}} [J(\mathbf{r})] \equiv -\hat{\Delta} + \frac{\delta E_{\text{Hxc}}^{\text{LDA}}}{\delta \rho(\mathbf{r})} + \frac{\delta E_{\text{ion}}}{\delta \rho(\mathbf{r})} + \sum_i \hat{H}_i^{\text{int}} - \sum_i V_i^{\text{dc}} \hat{N}_i^{\text{loc}}$$

An example: Orbital Differentiation with Crystal Field Effects in UO₂

UO₂ (arXiv:1606.09614 (2016))

Cubic fluorite structure

**Point symmetry U atoms
 "double O point group" (low symmetry)**



$$\begin{aligned}
 |\Gamma_6, 7/2, \pm\rangle &= \sqrt{5/12} |7/2, \pm 7/2\rangle + \sqrt{7/12} |7/2, \mp 1/2\rangle \\
 |\Gamma_7, 7/2, \pm\rangle &= \mp \sqrt{3/4} |7/2, \pm 5/2\rangle \pm \sqrt{1/4} |7/2, \mp 3/2\rangle \\
 |\Gamma_8^{(1)}, 7/2, \pm\rangle &= \pm \sqrt{7/12} |7/2, \pm 7/2\rangle \mp \sqrt{5/12} |7/2, \mp 1/2\rangle \\
 |\Gamma_8^{(2)}, 7/2, \pm\rangle &= \mp \sqrt{1/4} |7/2, \pm 5/2\rangle \mp \sqrt{3/4} |7/2, \mp 3/2\rangle \\
 |\Gamma_7, 5/2, \pm\rangle &= \sqrt{5/6} |5/2, \pm 3/2\rangle - \sqrt{1/6} |5/2, \mp 5/2\rangle \\
 |\Gamma_8^{(1)}, 5/2, \pm\rangle &= \sqrt{1/6} |5/2, \pm 3/2\rangle + \sqrt{5/6} |5/2, \mp 5/2\rangle \\
 |\Gamma_8^{(2)}, 5/2, \pm\rangle &= |5/2, \pm 1/2\rangle,
 \end{aligned}$$

Self Energy $\Sigma(\omega)$ non diagonal (less symmetry \rightarrow less selection rules)

An example: Orbital Differentiation with Crystal Field Effects in UO₂

UO₂ (arXiv:1606.09614 (2016))

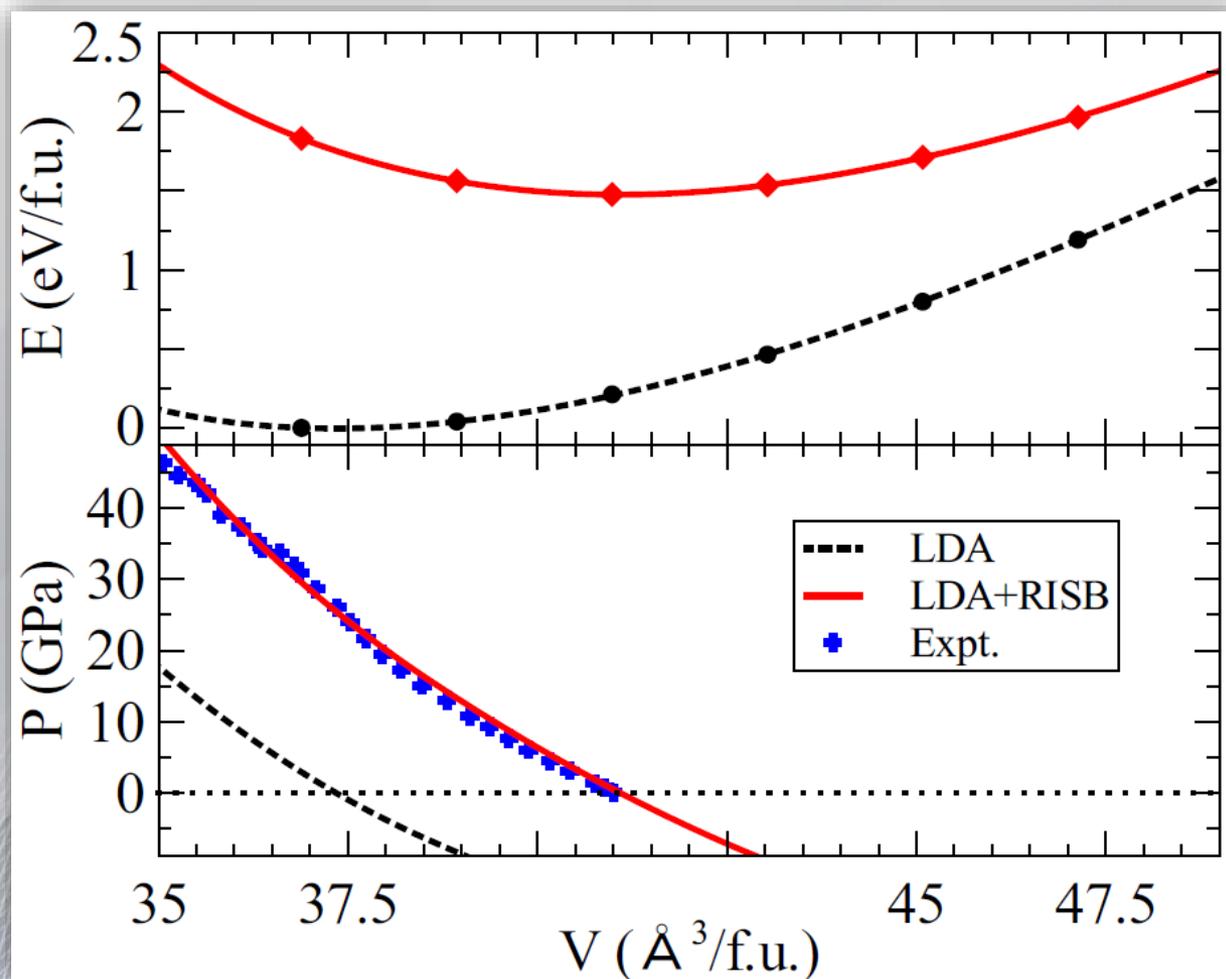
Eigenvalues of the 5*f* quasi-particle matrix *Z* and corresponding orbital occupations for LDA+RISB calculations. Theoretical results obtained by taking into account the crystal field splittings and by neglecting them.

Crystal Field Splitting essential in order to capture the correct pattern of orbital differentiation in UO₂

w/ CFS	$\Gamma_8(4)$	$\Gamma_7(2)$	$\Gamma_8(4)$	$\Gamma_7(2)$	$\Gamma_6(2)$
<i>Z</i>	0	0.92	0.92	0.95	0.95
<i>n</i>	1.92	0.14	0.08	0.06	0.04
w/o CFS				5/2	7/2
<i>Z</i>				0	0.96
<i>n</i>				1.98	0.16

An example: Orbital Differentiation with Crystal Field Effects in UO_2

UO_2 (arXiv:1606.09614 (2016))



An example: Polymorphism in Strongly Correlated Materials

Polymorphism

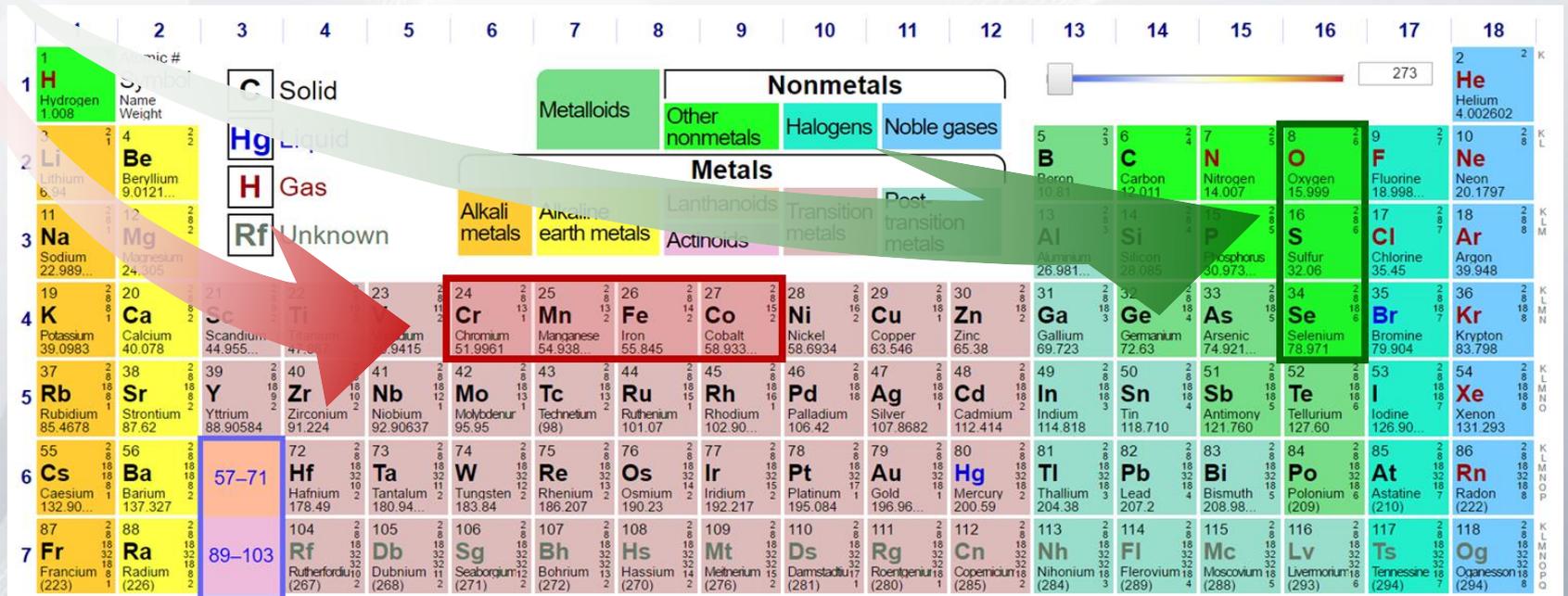
- ❖ **Carbon**: Graphite, Diamond (different mechanical, optical, electronic properties)
- ❖ **TiO₂**: Anatase, Rutile (enhance photocatalytic activity in Anatase with respect to Rutile)
- ❖ **White and Grey Tin** (different electronic and mechanical properties)

LDA-like functionals lead systematically to **wrong predictions** for correlated materials, e.g., involving transition-metal atoms.

An example: Polymorphism in Strongly Correlated Materials

Ground state structures and equilibrium volumes predicted by LDA and LDA+GA/RISB

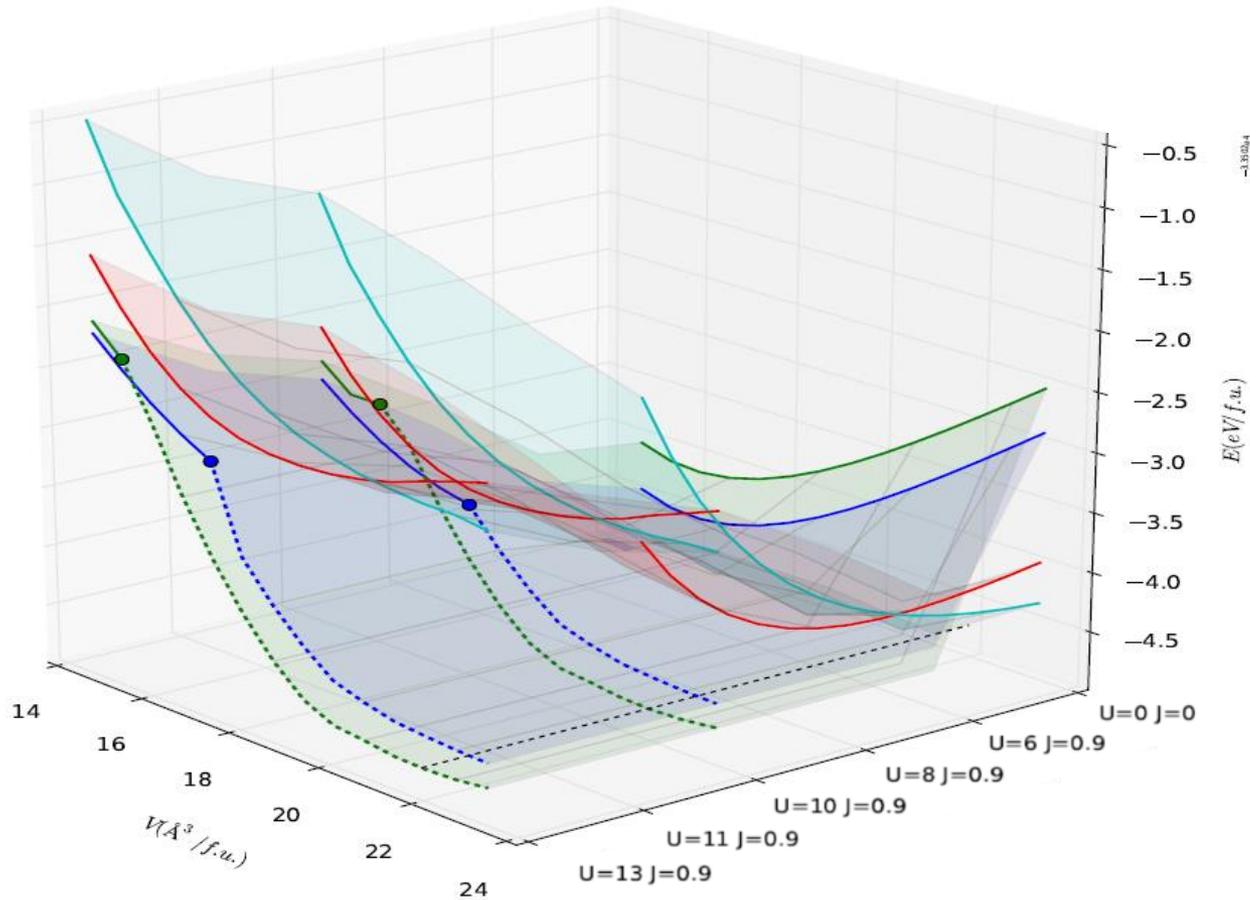
	LDA			LDA+SB $U = 13 J = 0.9$			experiment		
	g.s. structure	g.s. phase	V_0 ($\text{\AA}^3/f.u.$)	g.s. structure	g.s. phase	V_0 ($\text{\AA}^3/f.u.$)	g.s. structure	g.s. phase	V_0 ($\text{\AA}^3/f.u.$)
CoO	Wurtzite	Metal	17.64	Rocksalt	Insulator	20.48	Rocksalt	Insulator	19.35
CoS	NiAs	Metal	23.11	NiAs	Metal	25.93	NiAs	Metal	25.77
CoSe	NiAs	Metal	27.25	NiAs	Metal	30.99	NiAs	Metal	30.27
CrO	Wurtzite	Metal	17.64	Rocksalt	Metal	18.27	Rocksalt		18
MnO	Wurtzite	Metal	17.13	Rocksalt	Insulator	22.06	Rocksalt	Insulator	21.97
FeO	Zincblende	Metal	18.69	Rocksalt	Insulator	21.23	Rocksalt	Insulator	20.35



An example: Polymorphism in Strongly Correlated Materials

Energy Profile MnO

MnO energy – volume curves DFT + GA/RISB

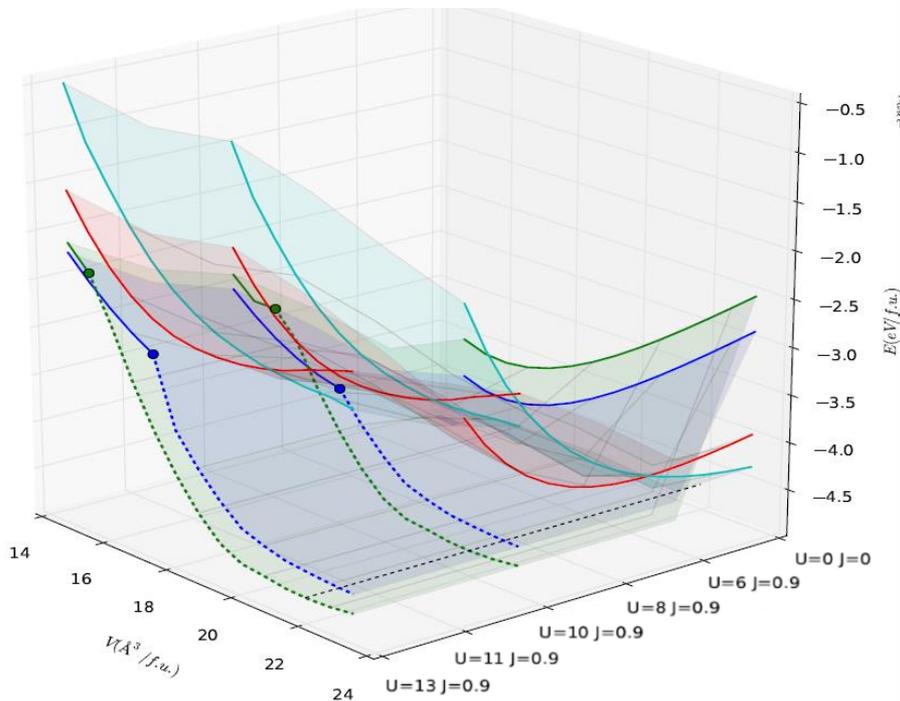


- Rocksalt Metal
- NiAs Metal
- Wurtzite Metal
- Zinblende Metal
- ⋯ Rocksalt Mott
- ⋯ NiAs Mott
- ⋯ $V_0 = 21.97 \text{\AA}^3$ / f.u.

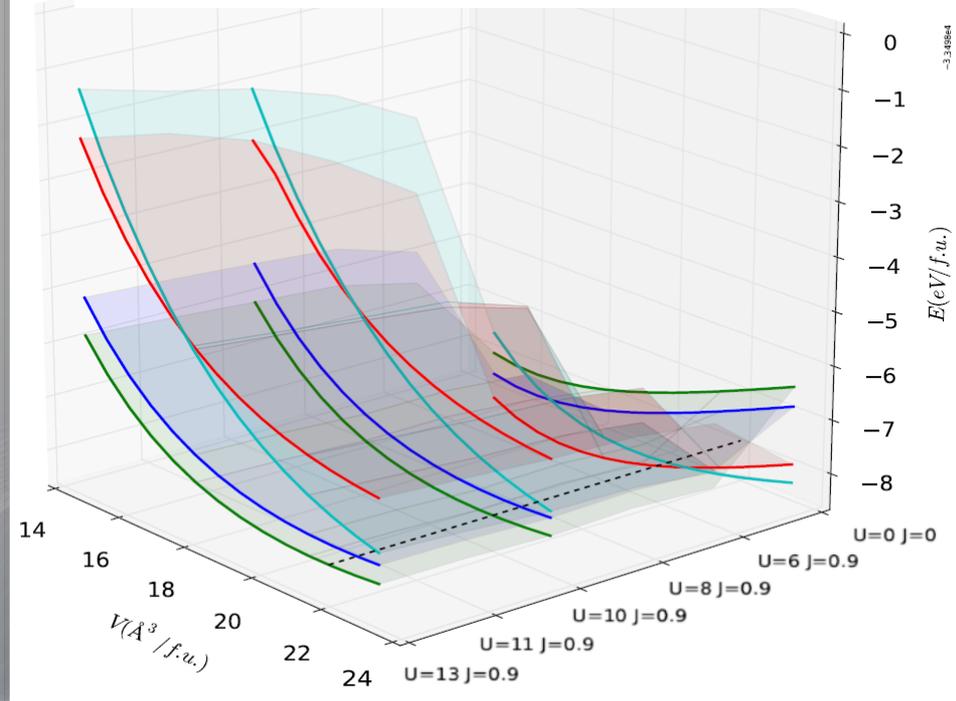
An example: Polymorphism in Strongly Correlated Materials

Energy Profile MnO

MnO energy – volume curves DFT + GA/RISB



MnO energy – volume curves DFT + U

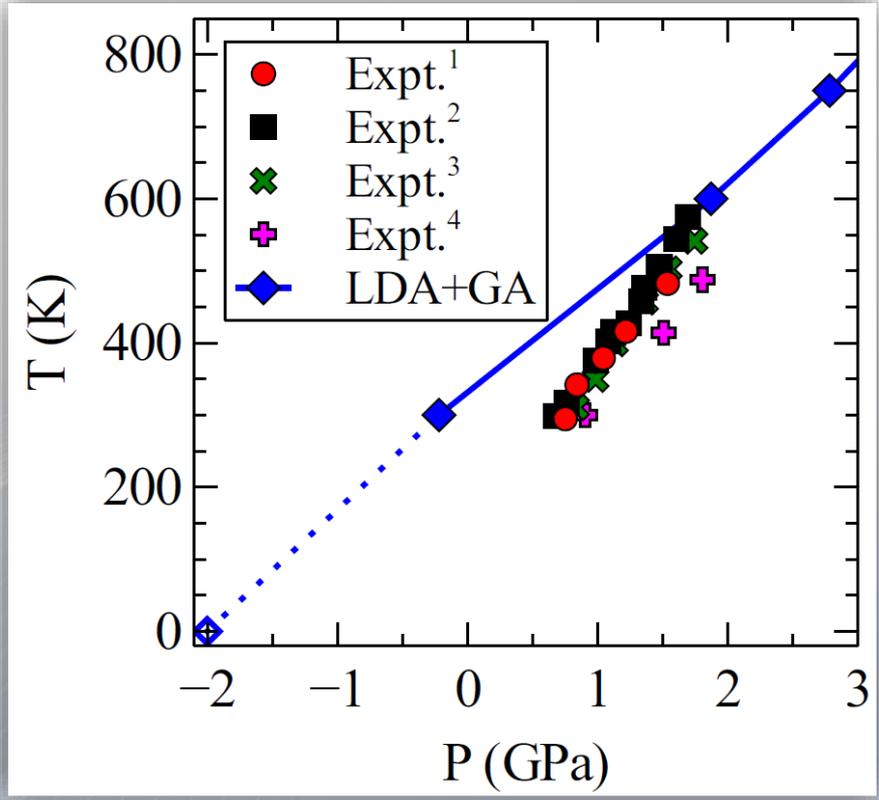
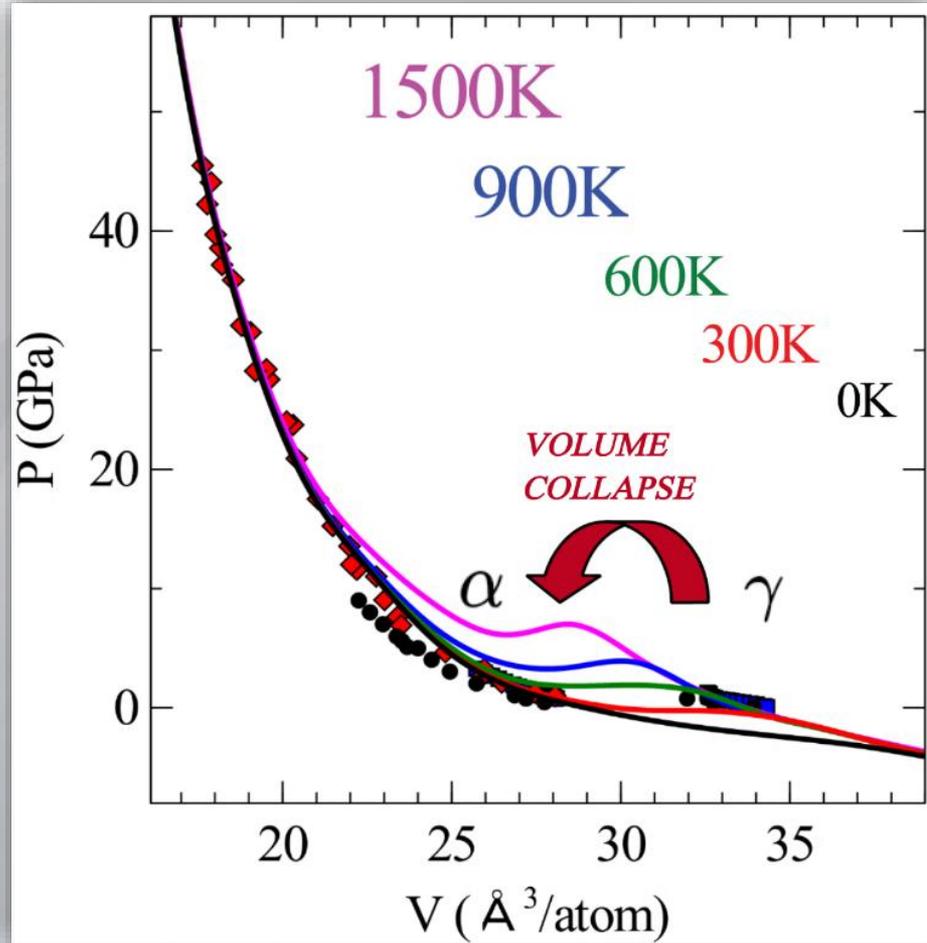


- | | |
|------------------|---|
| Rocksalt Metal | Rocksalt Mott |
| NiAs Metal | NiAs Mott |
| Wurtzite Metal | $V_0 = 21.97 \text{ \AA}^3 / \text{f.u.}$ |
| Zincblende Metal | |

**Thank you for your
attention!**

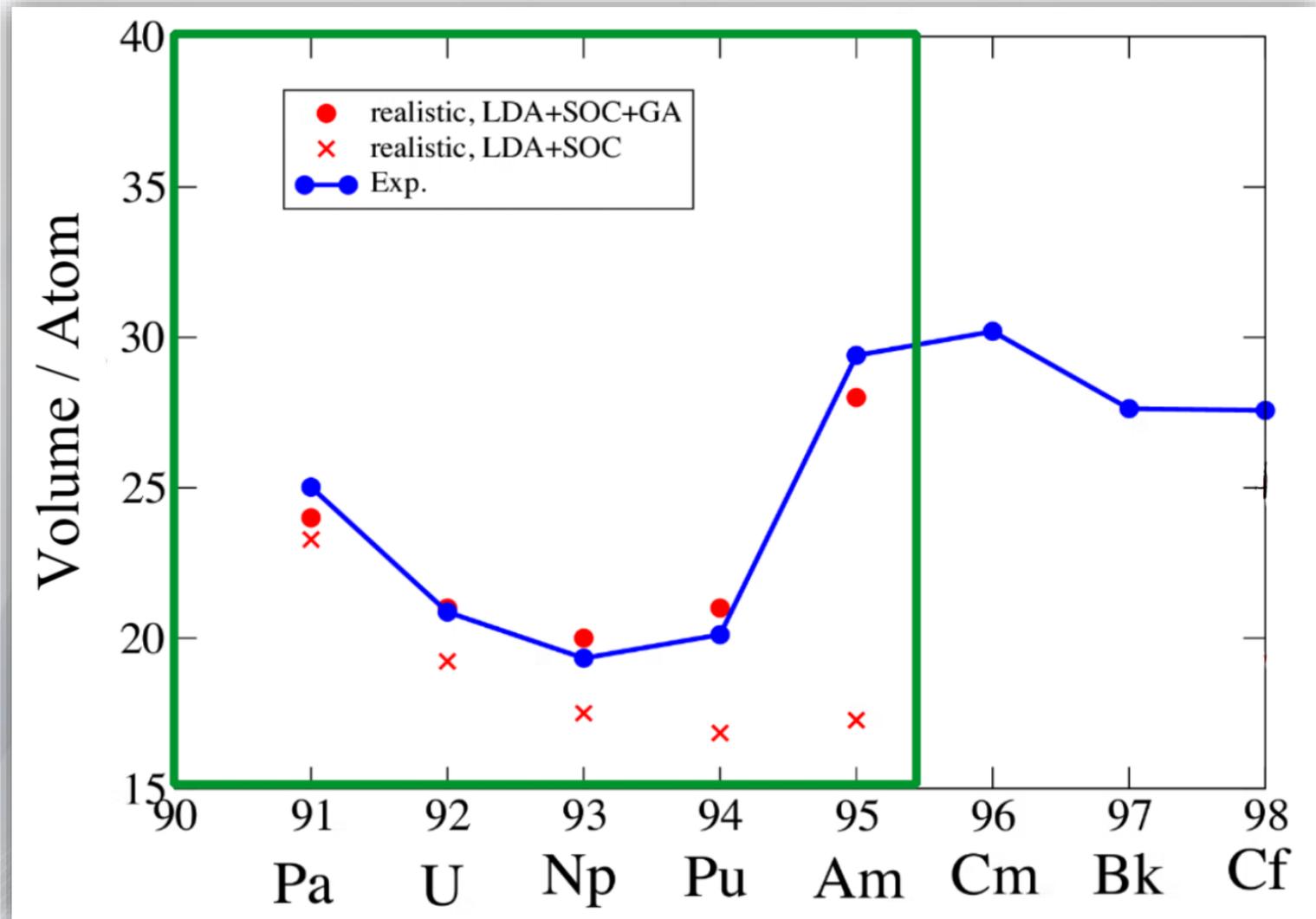
An example: The γ - α transition of Ce

**Phys. Rev. Lett. 111, 196801 (2013), Phys. Rev. B 90, 161104(R) (2014),
Phys. Rev. Lett. 113, 036402 (2014)**



Experimental data at room temperature

Actinides Transition



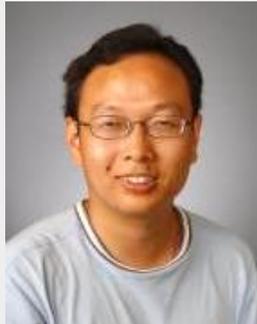
HANDS-ON SESSION

(assistant: Tsung-Han Lee)

**Using RISB Code Developed with Yongxin Yao (Iowa)
and Gabriel Kotliar (Rutgers):**

N. Lanatà, Y. Yao, C.-Z. Wang, K.-M. Ho, and G. Kotliar, PRX **5**, 011008 (2015)

N. Lanatà, Y. Yao, X. Deng, V. Dobrosavljevic and G. Kotliar, arXiv:1606.09614 (2016).



**Implementation of LAPW interface with the DFT WIEN2K code adapted
from DFT+DMFT code of:**

K. Haule et al., see Phys. Rev. B **81**, 195107 (2010).

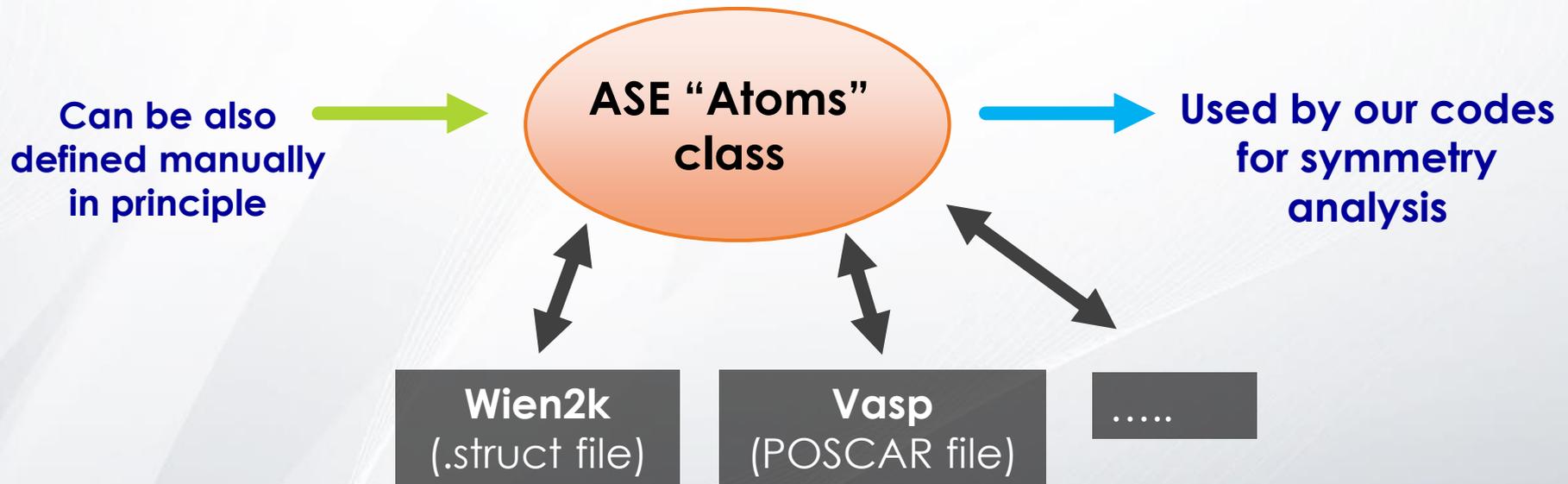


CyGutz User Guide

For details, please refer to CyGutz user guide:
<http://ykent.public.iastate.edu/cygutz/>

Fundamental object encoding material structure processed by our symmetry-analysis codes:

ASE (Atomic Simulation Environment, GNU LGPL license) class “Atoms”



In our DFT (Wien2k) + X (GA/RISB, DMFT,...) “Atoms” class automatically created from Wien2k structure file

But our symmetry codes elaborate the ASE (GNU LGPL license) “Atoms” class (which does not depend on Wien2k)

Example where “Atoms” class is created manually

```
lanata@Phoenix: ~/scratch/VideoConference/Preparation structure files
lanata@Phoenix: ~/scratch/VideoConference/Preparation structure files 103x33
File Edit Options Buffers Tools Python Help
import sys
import numpy as np
from numpy.linalg import det

Manual preparation “Atoms” class of MnBi

symbols=['Mn','Mn','Bi','Bi']
cell = [ (4.29, 0, 0), (0, 4.29, 0), (0, 0, 6.13) ]
scaled_positions=[(0,0,0), (0,0,1.0/2.0), (1.0/3.0,2.0/3.0,1.0/4.0), (2.0/3.0,1.0/3.0,3.0/4.0)]

from ase import Atoms
Material = Atoms( symbols=symbols, cell=cell, scaled_positions=scaled_positions, pbc=True )

#####

import os
from ase.io.wien2k import write_struct

path = os.getcwd()

material = 'MnBi'
name = material + '.struct'
fullname = path + '/' + material + '/' + name
print fullname

write_struct(name, atoms2=Material, rmt=None, lattice='P', zza=None)
```

Corresponding Wien2k structure file automatically written in proper format

Example where “Atoms” class is written/read from different structure files

lanata@Phoenix: ~/scratch/VideoConference/Preparation structure files

lanata@Phoenix: ~/scratch/VideoConference/Preparation structure files 103x33

File Edit Options Buffers Tools Python Help

```
import sys
import numpy as np
from numpy.linalg import det

from ase import Atoms
```

#####

```
import os
from ase.io.wien2k import write_struct
from ase.io import read
```

Creating “Atoms” classes from existing Vasp POSCAR files

```
Mn0_RS = read('POSCAR_Mn0_RS', index=None, format='vasp')
```

```
Mn0_ZB = read('POSCAR_Mn0_ZB', index=None, format='vasp')
```

```
write_struct('Mn0_RS.struct', atoms2=Mn0_RS, rmt=None, lattice='P', zza=None)
```

```
write_struct('Mn0_ZB.struct', atoms2=Mn0_ZB, rmt=None, lattice='P', zza=None)
```

Corresponding Wien2k structure files automatically written from “Atoms” classes

-UU-:----F1 convert_struct.py All L23 (Python) -----

End of buffer

Work done by our symmetry code: Part 1

Detect: (I) symmetry group lattice, (II) equivalent atoms in unit cell, (III) point symmetry groups of inequivalent correlated atoms (3x3 matrices representing 3-dimensional space isometries).

“Easy”: Essentially real-space geometry.
Automatically done by “pymatgen” (ASE-based open-source software)

Starting point for actual symmetry analysis (see the next slide).

Work done by our symmetry code: Part 2

Use theory of group representations to split single-particle space and many-body local space of strongly correlated electrons in irreducible representations.

More complicated: Depends on whether we treat “d” or “f” electrons, whether we neglect or not SOC/CF, single-particle space or many-body space, etc... In general. It depends on how the quantum configurations considered transform with respect to the group transformations. Additional complications of “double groups” (2π rotations not identity for half-integer J).

This enables us to obtain: (I) “symmetry basis” in which the local self-energy and the many-body local density matrix of the correlated electrons are as simple as possible (block diagonal, inequivalent representations not coupled, ecc...).

Interactive user interface

Given a folder with a completed DFT job, the python script “init_ga.py” asks questions to the user concerning the desired approximations.

(The symmetry analysis depends on whether the correlated shell is “d” or “f” and whether the SOC or the CFS are negligible)

Examples:

◆ If SOC is neglected a rotation within the single-particle (or many-body) space is represented as $\exp(\mathbf{iL}\theta)$, where \mathbf{L} is the orbital angular momentum. If instead both SOC and CFS are important, a rotation within the same space is represented as $\exp(\mathbf{iJ}\theta)$, where $\mathbf{J}=\mathbf{L}+\mathbf{S}$ is the total angular momentum.

◆ If J is half-integer a rotation of 2π is not the identity (but the identity multiplied by -1). This requires to duplicate the group (double groups). For instance, the Koster symbols in our paper about UO_2 [arXiv:1606.09614 (2016)] correspond to irreducible representations of a double group.

Our code can deal with all of these possibilities automatically. The user does not need to know anything about group theory, but simply describe the physical problem and the desired approximation scheme.

Initialization UO_2 : LDA

Initialization UO₂ : LDA

```
henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... ×  
henhans@henhans-Satellite-C55-C:~/cygutz/U02/LDA_k2000/U02$ init_lapw -b -vxc 5 -ecut 8 -rkmax 9 -numk 2000
```

Initialization UO₂ : LDA

henhans@henhans-Satellite-C55-C: ~

× henhans@henhans-Satellite-C55-C: ~/cygutz/UO2/LDA/UO2 ×

henhans@henhans-Satellite-C55-C: ~/git/cygutz_release/t... ×

```
ATOM 2 O          ATOM 1 U
RMT( 2)=2.09000 AND RMT( 1)=2.36000
SUMS TO 4.45000 LT. NN-DIST= 4.47760
NN ENDS
0.0u 0.0s 0:00.00 0.0% 0+0k 0+40io 0pf+0w
> sgroup (12:51:05) 0.0u 0.0s 0:00.00 0.0% 0+0k 0+8io 0pf+0w
Names of point group: m-3m 4/m -3 2/m 0h
Names of point group: -43m -43m Td
Number and name of space group: 225 (F m -3 m)
> symmetry (12:51:05) 0.0u 0.0s 0:00.00 0.0% 0+0k 0+72io 0pf+0w
2 Atoms found: U O
generate atomic configuration for atom 1 : U
generate atomic configuration for atom 2 : O
SELECT XCPOT:
recommended: 13: PBE-GGA (Perdew-Burke-Ernzerhof 96)
              5: LSDA
              11: WC-GGA (Wu-Cohen 2006)
              19: PBEsol-GGA (Perdew etal. 2008)
SELECT ENERGY to separate core and valence states:
recommended: -6.0 Ry (check how much core charge leaks out of MT-sphere)
ALTERNATIVELY: specify charge localization
(between 0.97 and 1.0) to select core state

WARNING: R0=0.000100 for atom 1 Z= 92.00 too big. Use 0.00005

LSTART ENDS
WARNING: R0=0.000100 for atom 1 Z= 92.00 too big. Use 0.00005
> inputfiles prepared (12:51:05)
NUMBER OF K-POINTS IN WHOLE CELL: (0 allows to specify 3 divisions of G)
length of reciprocal lattice vectors: 1.052 1.052 1.052 17.100 17.100 17.100
165 k-points generated, ndiv= 17 17 17
KGEN ENDS
> dstart (12:51:05) DSTART ENDS
0.9u 0.0s 0:00.99 98.9% 0+0k 0+424io 0pf+0w
----> new UO2.in0 generated
init_lapw finished ok

henhans@henhans-Satellite-C55-C:~/cygutz/UO2/LDA/UO2$ initso_lapw █
```

Initialization UO₂ : LDA

henhans@henhans-Satellite-C55-C: ~

× henhans@henhans-Satellite-C55-C: ~/cygutz/UO2/LDA/UO2 ×

henhans@henhans-Satellite-C55-C: ~/git/cygutz_release/t... ×

The file UO2.in2c has been generated automatically

```
---->Please select the direction of the moment ( h k l )  
(For R-lattice in R coordinates)(default 0 0 1): █
```

Initialization UO₂ : LDA

henhans@henhans-Satellite-C55-C: ~

× henhans@henhans-Satellite-C55-C: ~/cygutz/UO2/LDA/UO2 ×

henhans@henhans-Satellite-C55-C: ~/git/cygutz_release/t... ×

The file UO2.in2c has been generated automatically

---->Please select the direction of the moment (h k l)
(For R-lattice in R coordinates)(default 0 0 1):

atom 1 is U
atom 2 is O

Select atom-numbers (1,2,3) or "ranges of atoms" (1-3,9-12) (without blanks)
for which you would NOT like to add SO interaction
(default none, just press "enter"): 1

Initialization UO₂ : LDA

henhans@henhans-Satellite-C55-C: ~

×

henhans@henhans-Satellite-C55-C: ~/cygutuz/UO2/LDA/UO2

×

henhans@henhans-Satellite-C55-C: ~/git/cygutz_release/t...

×

```
For large spin orbit effects it might be necessary to include many more
eigenstates from lapw1 by increasing EMAX in case.in1(c).
```

```
---->Please enter EMAX(default 5.0 Ryd): █
```

Initialization UO₂ : LDA

henhans@henhans-Satellite-C55-C: ~

× henhans@henhans-Satellite-C55-C: ~/cygutz/UO2/LDA/UO2 ×

henhans@henhans-Satellite-C55-C: ~/git/cygutz_release/t... ×

```
For large spin orbit effects it might be necessary to include many more
eigenstates from lapw1 by increasing EMAX in case.in1(c).
```

```
---->Please enter EMAX(default 5.0 Ryd):
```

```
The radial basis set for heavy atoms with p-semicore states is very
limited. One can improve this by adding RLOs. Note: you MUST NOT add
RLOs for atoms like oxygen,... therefore the default is set to NONE
```

```
---->Add RLO for NONE, ALL, CHOOSE elements? (N/a/c) : █
```

Initialization UO₂ : LDA

henhans@henhans-Satellite-C55-C: ~

× henhans@henhans-Satellite-C55-C: ~/cygutz/UO2/LDA/UO2 ×

henhans@henhans-Satellite-C55-C: ~/git/cygutz_release/t... ×

For large spin orbit effects it might be necessary to include many more eigenstates from lapw1 by increasing EMAX in case.in1(c).

---->Please enter EMAX(default 5.0 Ryd):

The radial basis set for heavy atoms with p-semicore states is very limited. One can improve this by adding RLOs. Note: you MUST NOT add RLOs for atoms like oxygen,... therefore the default is set to NONE

---->Add RLO for NONE, ALL, CHOOSE elements? (N/a/c) :

cat: .ieds: No such file or directory

Check the generated UO2.inso file (RLOs,...)

Check the generated UO2.in1 file (Emax at the bottom of the file)

In spinpolarized case SO may reduce symmetry.

The program symmetso dedects the proper symmetry and creates new struct and input files. (Note, equivalent atoms could become inequivalent in some cases).

Do you have a spinpolarized case (and want to run symmetso) ? (y/N)

Initialization UO₂ : LDA

```
henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... × henhans@henhans-Satel... ×  
henhans@henhans-Satellite-C55-C:~/cygutz/U02/LDA_k2000/U02$ run_lapw -so
```

**Initialization UO_2 :
LDA + RISB**

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> ls
dstart.def          params.dat          UO2.in2_ls         UO2.kgen           UO2.rspdn          UO2.vspdn_st
dstart.error        symmetry.def        UO2.in2_st         UO2.klist          UO2.rspup          UO2.vsp_st
GL.INP              UO2.bva            UO2.in2_sy         UO2.nnshells       UO2.sigma          WH_HS.INP
init_ga_info.h5     UO2.clmsum         UO2.inc            UO2.outputd        UO2.struct         WH_HS.INP_ORIG
init_ga.input       UO2.dayfile        UO2.inc_st         UO2.outputtkgen    UO2.struct_nn      WH_N2N.INP
init_ga.slog        UO2.in0            UO2.inm            UO2.outputnn       UO2.struct_orig    WH_SIGMA_STRUCT.INP
input.slog          UO2.in0_st         UO2.inm_restart_st UO2.outputs        UO2.struct_setrmt  WH_SL_VEC.INP
kgen.def            UO2.in0_std        UO2.inm_st         UO2.outputsgroup   UO2.struct_sgroup
:log                UO2.in1            UO2.inq            UO2.outputsgroup1  UO2.struct_st
lstart.def          UO2.in1_st         UO2.inq_st         UO2.outputst       UO2.test
new_super.clmsum    UO2.in2            UO2.inso           UO2.rsigma          UO2.tmp
nn.def              UO2.in2c           UO2.inst           UO2.rsp             UO2.tmpden
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> init_ga.py
```

Running script “init_ga.py” in folder with completed DFT run

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> ls
dstart.def          params.dat          UO2.in2_ls         UO2.kgen           UO2.rspdn          UO2.vspdn_st
dstart.error        symmetry.def        UO2.in2_st         UO2.klist          UO2.rspup          UO2.vsp_st
GL.INP              UO2.bva            UO2.in2_sy         UO2.nnshells       UO2.sigma          WH_HS.INP
init_ga_info.h5     UO2.clmsum         UO2.inc            UO2.outputd        UO2.struct         WH_HS.INP_ORIG
init_ga.input        UO2.dayfile        UO2.inc_st         UO2.outputkgen     UO2.struct_nn      WH_N2N.INP
init_ga.slog         UO2.in0            UO2.inm            UO2.outputnn       UO2.struct_orig    WH_SIGMA_STRUCT.INP
input.slog           UO2.in0_st         UO2.inm_restart_st UO2.outputs        UO2.struct_setrmt  WH_SL_VEC.INP
kgen.def            UO2.in0_std        UO2.inm_st         UO2.outputsgroup   UO2.struct_sgroup
:log                 UO2.in1            UO2.inq            UO2.outputsgroup1  UO2.struct_st
lstart.def           UO2.in1_st         UO2.inq_st         UO2.outputst        UO2.test
new_super.clmsum     UO2.in2            UO2.inso           UO2.rsigma          UO2.tmp
nn.def               UO2.in2c           UO2.inst           UO2.rsp             UO2.tmpden
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> init_ga.py

User inputs to initialize the ga job.

Do you want to BREAK SPIN-SYMMETRY?
Pick one from [y, n]...n
```

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> ls
dstart.def          params.dat          UO2.in2_ls         UO2.kgen           UO2.rspdn          UO2.vspdn_st
dstart.error        symmetry.def        UO2.in2_st         UO2.klist          UO2.rspup          UO2.vsp_st
GL.INP              UO2.bva            UO2.in2_sy         UO2.nnshells       UO2.sigma          WH_HS.INP
init_ga_info.h5     UO2.clmsum         UO2.inc            UO2.outputd        UO2.struct         WH_HS.INP_ORIG
init_ga.input        UO2.dayfile        UO2.inc_st         UO2.outputkgen     UO2.struct_nn      WH_N2N.INP
init_ga.slog         UO2.in0            UO2.inm            UO2.outputnn       UO2.struct_orig    WH_SIGMA_STRUCT.INP
input.slog           UO2.in0_st         UO2.inm_restart_st UO2.outputs        UO2.struct_setrmt  WH_SL_VEC.INP
kgen.def            UO2.in0_std        UO2.inm_st         UO2.outputsgroup   UO2.struct_sgroup
:log                 UO2.in1            UO2.inq            UO2.outputsgroup1  UO2.struct_st
lstart.def           UO2.in1_st         UO2.inq_st         UO2.outputst       UO2.test
new_super.clmsum    UO2.in2            UO2.inso           UO2.rsigma          UO2.tmp
nn.def               UO2.in2c           UO2.inst           UO2.rsp             UO2.tmpden

lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> init_ga.py

User inputs to initialize the ga job.

Do you want to BREAK SPIN-SYMMETRY?
Pick one from [y, n]...n

Do you want to COMPLETELY BREAK ORBITAL-SYMMETRY?
Pick one from [y, n]...n
```

Answer “y” only if looking for solution breaking local spin/orbital symmetry spontaneously (e.g., we may need it for URu₂Si₂)

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> ls
dstart.def          params.dat          UO2.in2_ls         UO2.kgen           UO2.rspdn          UO2.vspdn_st
dstart.error        symmetry.def        UO2.in2_st         UO2.klist          UO2.rspup          UO2.vsp_st
GL.INP              UO2.bva            UO2.in2_sy         UO2.nnshells       UO2.sigma          WH_HS.INP
init_ga_info.h5     UO2.clmsum         UO2.inc            UO2.outputd        UO2.struct         WH_HS.INP_ORIG
init_ga.input        UO2.dayfile        UO2.inc_st         UO2.outputkgen     UO2.struct_nn      WH_N2N.INP
init_ga.slog         UO2.in0            UO2.inm            UO2.outputnn       UO2.struct_orig    WH_SIGMA_STRUCT.INP
input.slog           UO2.in0_st         UO2.inm_restart_st UO2.outputps       UO2.struct_setrmt  WH_SL_VEC.INP
kgen.def            UO2.in0_std        UO2.inm_st         UO2.outputsgroup   UO2.struct_sgroup
:log                 UO2.in1            UO2.inq            UO2.outputsgroup1  UO2.struct_st
lstart.def           UO2.in1_st         UO2.inq_st         UO2.outputst        UO2.test
new_super.clmsum    UO2.in2            UO2.inso           UO2.rsigma          UO2.tmp
nn.def               UO2.in2c           UO2.inst           UO2.rsp             UO2.tmpden
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> init_ga.py

User inputs to initialize the ga job.

Do you want to BREAK SPIN-SYMMETRY?
Pick one from [y, n]...n

Do you want to COMPLETELY BREAK ORBITAL-SYMMETRY?
Pick one from [y, n]...n

Symmetrically-equivalent atom indices:  0 1 1
(note: '0 0 0 1 1' means 1-3 and 4-5 are two inequivalent atoms).
Accept?
Pick one from [y, n]...y
```

Pymatgen detects automatically equivalent atoms (information used to avoid solving repeatedly equivalent impurity problems)

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> ls
dstart.def          params.dat          UO2.in2_ls         UO2.kgen           UO2.rspdn          UO2.vspdn_st
dstart.error        symmetry.def        UO2.in2_st         UO2.klist          UO2.rspup          UO2.vsp_st
GL.INP              UO2.bva            UO2.in2_sy         UO2.nnshells       UO2.sigma          WH_HS.INP
init_ga_info.h5     UO2.clmsum         UO2.inc            UO2.outputd        UO2.struct         WH_HS.INP_ORIG
init_ga.input        UO2.dayfile        UO2.inc_st         UO2.outputkgen     UO2.struct_nn      WH_N2N.INP
init_ga.slog         UO2.in0            UO2.inm            UO2.outputnn       UO2.struct_orig    WH_SIGMA_STRUCT.INP
input.slog           UO2.in0_st         UO2.inm_restart_st UO2.outputs        UO2.struct_setrmt  WH_SL_VEC.INP
kgen.def            UO2.in0_std        UO2.inm_st         UO2.outputsgroup   UO2.struct_sgroup
:log                 UO2.in1            UO2.inq            UO2.outputsgroup1  UO2.struct_st
lstart.def           UO2.in1_st         UO2.inq_st         UO2.outputst       UO2.test
new_super.clmsum    UO2.in2            UO2.inso           UO2.rsigma          UO2.tmp
nn.def              UO2.in2c           UO2.inst           UO2.rsp             UO2.tmpden
```

User inputs to initialize the ga job.

Do you want to BREAK SPIN-SYMMETRY?

Pick one from [y, n]...n

Do you want to COMPLETELY BREAK ORBITAL-SYMMETRY?

Pick one from [y, n]...n

Symmetrically-equivalent atom indices: 0 1 1
(note: '0 0 0 1 1' means 1-3 and 4-5 are two inequivalent atoms).

Accept?

Pick one from [y, n]...y

```
-----
atom 0  U
Is this atom correlated?
Pick one from [y, n]...y
```

Code asking user if atom with label “0” (which is U) is correlated or not

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> ls
dstart.def          params.dat          UO2.in2_ls         UO2.kgen           UO2.rspdn          UO2.vspdn_st
dstart.error        symmetry.def        UO2.in2_st         UO2.klist          UO2.rspup          UO2.vsp_st
GL.INP              UO2.bva            UO2.in2_sy         UO2.nnshells       UO2.sigma          WH_HS.INP
init_ga_info.h5     UO2.clmsum         UO2.inc            UO2.outputd        UO2.struct         WH_HS.INP_ORIG
init_ga.input        UO2.dayfile        UO2.inc_st         UO2.outputkgen     UO2.struct_nn      WH_N2N.INP
init_ga.slog         UO2.in0            UO2.inm            UO2.outputnn       UO2.struct_orig    WH_SIGMA_STRUCT.INP
input.slog           UO2.in0_st         UO2.inm_restart_st UO2.outputs        UO2.struct_setrmt  WH_SL_VEC.INP
kgen.def             UO2.in0_std        UO2.inm_st         UO2.outputsgroup   UO2.struct_sgroup
:log                 UO2.in1            UO2.inq            UO2.outputsgroup1  UO2.struct_st
lstart.def           UO2.in1_st         UO2.inq_st         UO2.outputst       UO2.test
new_super.clmsum     UO2.in2            UO2.inso           UO2.rsigma          UO2.tmp
nn.def               UO2.in2c           UO2.inst           UO2.rsp             UO2.tmpden
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> init_ga.py

User inputs to initialize the ga job.

Do you want to BREAK SPIN-SYMMETRY?
Pick one from [y, n]...n

Do you want to COMPLETELY BREAK ORBITAL-SYMMETRY?
Pick one from [y, n]...n

Symmetrically-equivalent atom indices:  0  1  1
(note: '0 0 0 1 1' means 1-3 and 4-5 are two inequivalent atoms).
Accept?
Pick one from [y, n]...y

-----
atom  0  U

Is this atom correlated?
Pick one from [y, n]...y

Enter correlated shells?
Pick one or combinations separated by blank space
from [s, p, d, f]...f
```

U atom has f correlated electrons

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/.w/test_UO2/LDA/UO2
lanata@rupc04:~/.w/test_UO2/LDA/UO2 118x37
init_ga.slog      UO2.in0      UO2.inm      UO2.outputnn  UO2.struct_orig  WH_SIGMA_STRUCT.INP
input.slog       UO2.in0_st   UO2.inm_restart_st  UO2.outputs     UO2.struct_setrmt  WH_SL_VEC.INP
kgen.def         UO2.in0_std  UO2.inm_st    UO2.outputsgroup  UO2.struct_sgroup
:log            UO2.in1      UO2.inq      UO2.outputsgroup1  UO2.struct_st
lstart.def       UO2.in1_st   UO2.inq_st    UO2.outputst      UO2.test
new_super.clmsum UO2.in2      UO2.inso     UO2.rsigma        UO2.tmp
nn.def          UO2.in2c     UO2.inst     UO2.rsp           UO2.tmpden
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> init_ga.py

User inputs to initialize the ga job.

Do you want to BREAK SPIN-SYMMETRY?
Pick one from [y, n]...n

Do you want to COMPLETELY BREAK ORBITAL-SYMMETRY?
Pick one from [y, n]...n

Symmetrically-equivalent atom indices:  0  1  1
(note: '0 0 0 1 1' means 1-3 and 4-5 are two inequivalent atoms).
Accept?
Pick one from [y, n]...y

-----
atom  0  U

Is this atom correlated?
Pick one from [y, n]...y

Enter correlated shells?
Pick one or combinations separated by blank space
from [s, p, d, f]...f

Do you want to take into account the SPIN-ORBIT interaction?
Pick one from [y, n]...y

Do you want to take into account the CRYSTAL FIELD effect?
Pick one from [y, n]...y
```

SOC and CFS not negligible: System not spin rotationally-invariant. Discrete group with rotations generated by $J=L+S$

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/.w/test_UO2/LDA/UO2
lanata@rupc04:~/.w/test_UO2/LDA/UO2 118x37
nn.def          UO2.in2c      UO2.inst      UO2.rsp      UO2.tmpden
lanata@rupc04:~/.mnt/w/test_UO2/LDA/UO2> init_ga.py

User inputs to initialize the ga job.

Do you want to BREAK SPIN-SYMMETRY?
Pick one from [y, n]...n

Do you want to COMPLETELY BREAK ORBITAL-SYMMETRY?
Pick one from [y, n]...n

Symmetrically-equivalent atom indices:  0  1  1
(note: '0 0 0 1 1' means 1-3 and 4-5 are two inequivalent atoms).
Accept?
Pick one from [y, n]...y

-----
atom  0  U

Is this atom correlated?
Pick one from [y, n]...y

Enter correlated shells?
Pick one or combinations separated by blank space
from [s, p, d, f]...f

Do you want to take into account the SPIN-ORBIT interaction?
Pick one from [y, n]...y

Do you want to take into account the CRYSTAL FIELD effect?
Pick one from [y, n]...y

-----
atom  1  O

Is this atom correlated?
Pick one from [y, n]...n
```

Code asking user if atom with label “1” (which is O) is correlated or not (it’s not)

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:...w/test_UO2/LDA/UO2
lanata@rupc04:...w/test_UO2/LDA/UO2 118x37
Accept?
Pick one from [y, n]...y

-----
atom 0  U

Is this atom correlated?
Pick one from [y, n]...y

Enter correlated shells?
Pick one or combinations separated by blank space
from [s, p, d, f]...f

Do you want to take into account the SPIN-ORBIT interaction?
Pick one from [y, n]...y

Do you want to take into account the CRYSTAL FIELD effect?
Pick one from [y, n]...y

-----
atom 1  O

Is this atom correlated?
Pick one from [y, n]...n

LHUB = 1: Slater-Condo parametrization.
      2: Kanamori parametrization (useful for models).
      0: U_{i,j,k,l} (NO SPIN INDEX) =
          int {dr int {dr' phi^{*}(r_i) phi^{*}(r'_j)
          V(|r-r'|) phi(r_k) phi(r'_l)}}
          will be provided by file V2A0.INP
     -1: U_{i,j,k,l} (INCLUDING SPIN INDEX) =
          int {dr int {dr' phi^{*}(r_i) phi^{*}(r'_j)
          phi(r_k) phi(r'_l)}}
          will be provided by file V2H.INP

Please select LHUB:
Pick one from [1, -1, 0, 2]...1
```

Other questions not related
with symmetry analysis

We choose Slater parametrization local
interaction (consequently values of U,J
will be asked)

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:...w/test_UO2/LDA/UO2
lanata@rupc04:...w/test_UO2/LDA/UO2 118x37
```

```
Do you want to take into account the SPIN-ORBIT interaction?
Pick one from [y, n]...y
```

```
Do you want to take into account the CRYSTAL FIELD effect?
Pick one from [y, n]...y
```

```
-----
atom 1 0
```

```
Is this atom correlated?
Pick one from [y, n]...n
```

```
LHUB = 1: Slater-Condo parametrization.
      2: Kanamori parametrization (useful for models).
      0: U_{i,j,k,l} (NO SPIN INDEX) =
         int {dr int {dr' phi^{*}(r_i) phi^{*}(r'_j)
         V(|r-r'|) phi(r_k) phi(r'_l)}}
         will be provided by file V2A0.INP
     -1: U_{i,j,k,l} (INCLUDING SPIN INDEX) =
         int {dr int {dr' phi^{*}(r_i) phi^{*}(r'_j)
         phi(r_k) phi(r'_l)}}
         will be provided by file V2H.INP
```

```
Please select LHUB:
Pick one from [1, -1, 0, 2]...1
```

```
LDC = 12: Recommended. Standard double counting
         (updating Vdc at each charge iteration,
         initial n0 to be provided.)
      2: Fix double counting potential
         (keep same Vdc/n0 at each charge iteration,
         n0 to be provided.)
      1: Standard double counting potential
         (n0 self-consistently determined.)
      0: No double counting.
```

```
Please select LDC:
Pick one from [12, 0, 1, 2]...12
```

Other questions not related
with symmetry analysis

We generally choose standard
(quadratic) double counting in all of our
calculations

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:...w/test_UO2/LDA/UO2
lanata@rupc04:...w/test_UO2/LDA/UO2 118x37
```

```
Do you want to take into account the CRYSTAL FIELD effect?
Pick one from [y, n]...y
```

```
-----
atom 1 0
```

```
Is this atom correlated?
Pick one from [y, n]...n
```

```
LHUB = 1: Slater-Condo parametrization.
       2: Kanamori parametrization (useful for models).
       0: U_{i,j,k,l} (NO SPIN INDEX) =
          int_{dr} int_{dr'} phi^{*}(r_i) phi^{*}(r'_j)
          V(|r-r'|) phi(r_k) phi(r'_l)}
          will be provided by file V2A0.INP
      -1: U_{i,j,k,l} (INCLUDING SPIN INDEX) =
          int_{dr} int_{dr'} phi^{*}(r_i) phi^{*}(r'_j)
          phi(r_k) phi(r'_l)}
          will be provided by file V2H.INP
```

```
Please select LHUB:
Pick one from [1, -1, 0, 2]...1
```

```
LDC = 12: Recommended. Standard double counting
          (updating Vdc at each charge iteration,
          initial n0 to be provided.)
       2: Fix double counting potential
          (keep same Vdc/n0 at each charge iteration,
          n0 to be provided.)
       1: Standard double counting potential
          (n0 self-consistently determined.)
       0: No double counting.
```

```
Please select LDC:
Pick one from [12, 0, 1, 2]...12
```

```
Please enter the tolerance of solving the equations of {R, \lambda}
(recommend 1.e-5 or smaller)...5.e-6
```

Other questions not related
with symmetry analysis

Question specific for GA/RISB solver
(precision requested for self-energy self
consistency, which is formulated as a root
problem)

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:...w/test_UO2/LDA/UO2
lanata@rupc04:...w/test_UO2/LDA/UO2 118x37
```

```
Is this atom correlated?
Pick one from [y, n]...n
```

```
LHUB = 1: Slater-Condo parametrization.
      2: Kanamori parametrization (useful for models).
      0: U_{i,j,k,l} (NO SPIN INDEX) =
      int {dr int {dr' phi^{*}(r_i) phi^{*}(r'_j)
      V(|r-r'|) phi(r_k) phi(r'_l)}}
      will be provided by file V2A0.INP
     -1: U_{i,j,k,l} (INCLUDING SPIN INDEX) =
      int {dr int {dr' phi^{*}(r_i) phi^{*}(r'_j)
      phi(r_k) phi(r'_l)}}
      will be provided by file V2H.INP
```

```
Please select LHUB:
Pick one from [1, -1, 0, 2]...1
```

```
LDC = 12: Recommended. Standard double counting
          (updating Vdc at each charge iteration,
          initial n0 to be provided.)
      2: Fix double counting potential
          (keep same Vdc/n0 at each charge iteration,
          n0 to be provided.)
      1: Standard double counting potential
          (n0 self-consistently determined.)
      0: No double counting.
```

```
Please select LDC:
Pick one from [12, 0, 1, 2]...12
```

```
Please enter the tolerance of solving the equations of {R, \lambda}
(recommend 1.e-5 or smaller)...5.e-6
```

```
LNEWTON = 0: Recommended. Modified Powell hybrid method (HYDRD1).
          -1: Broyden method. Faster for solutions with Z
              much larger than 0, e.g., magnetic calculations.
```

```
Please select LNEWTON:
Pick one from [-1, 0]...0
```

Other questions not related
with symmetry analysis

Question specific for GA/RISB solver
(solver used for root problem, basically
better to use default option in all cases)

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:...w/test_UO2/LDA/UO2
lanata@rupc04:...w/test_UO2/LDA/UO2 118x37
2: Kanamori parametrization (useful for models).
0: U_{i,j,k,l} (NO SPIN INDEX) =
  int_{dr} int_{dr'} phi^{*}(r_i) phi^{*}(r'_j)
  V(|r-r'|) phi(r_k) phi(r'_l)}
  will be provided by file V2A0.INP
-1: U_{i,j,k,l} (INCLUDING SPIN INDEX) =
  int_{dr} int_{dr'} phi^{*}(r_i) phi^{*}(r'_j)
  phi(r_k) phi(r'_l)}
  will be provided by file V2H.INP
Please select LHUB:
Pick one from [1, -1, 0, 2]...1

LDC = 12: Recommended. Standard double counting
  (updating Vdc at each charge iteration,
  initial n0 to be provided.)
2: Fix double counting potential
  (keep same Vdc/n0 at each charge iteration,
  n0 to be provided.)
1: Standard double counting potential
  (n0 self-consistently determined.)
0: No double counting.
Please select LDC:
Pick one from [12, 0, 1, 2]...12

Please enter the tolerance of solving the equations of {R, \lambda}
(recommend 1.e-5 or smaller)...5.e-6

LNEWTON = 0: Recommended. Modified Powell hybrid method (HYDRD1).
-1: Broyden method. Faster for solutions with Z
  much larger than 0, e.g., magnetic calculations.
Please select LNEWTON:
Pick one from [-1, 0]...0

LCLUSTER = 0: Single-atom impurity.
  1: Multi-atom (cluster) impurity.
Please select LCLUSTER:
Pick one from [0, 1]...0
```

Other questions not related
with symmetry analysis

The cluster impurity (option 1) is not even implemented. Answer “0” to apply standard single-site approximation scheme

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:...w/test_UO2/LDA/UO2
lanata@rupc04:...w/test_UO2/LDA/UO2 118x37
```

```
LDC = 12: Recommended. Standard double counting
          (updating Vdc at each charge iteration,
          initial n0 to be provided.)
  2: Fix double counting potential
          (keep same Vdc/n0 at each charge iteration,
          n0 to be provided.)
  1: Standard double counting potential
          (n0 self-consistently determined.)
  0: No double counting.
```

```
Please select LDC:
Pick one from [12, 0, 1, 2]...12
```

```
Please enter the tolerance of solving the equations of {R, \lambda}
(recommend 1.e-5 or smaller)...5.e-6
```

```
LNEWTON = 0: Recommended. Modified Powell hybrid method (HYDRD1).
          -1: Broyden method. Faster for solutions with Z
              much larger than 0, e.g., magnetic calculations.
```

```
Please select LNEWTON:
Pick one from [-1, 0]...0
```

```
LCLUSTER = 0: Single-atom impurity.
          1: Multi-atom (cluster) impurity.
```

```
Please select LCLUSTER:
Pick one from [0, 1]...0
```

```
Solution embedding system:
```

```
LEIGV = 0: Choose automatically solver depending
           on the size of the problem (DEFAULT)
  1: Exact diagonalization (ZHEEV) in LAPACK
  2: Lanczos (zhdrv1) in ARPACK
  3: Exact diagonalization (ZHEEVX,
           selective lowest two eigen-vectors) in LAPACK
  5: PRIMME (Recommended for large dimension.)
```

```
Please select LEIGV:
Pick one from [5, 0, 1, 2, 3]...5
```

Other questions not related
with symmetry analysis

Option “5” is basically a robust implementation of Lanczos (best option for now).

Currently testing new solvers (DMRG, CISD, etc....). Big room for improvement with respect to Lanczos.

Initialization UO₂ : LDA + RISB

lanata@rupc04:...w/test_UO2/LDA/UO2

lanata@rupc04:...w/test_UO2/LDA/UO2 118x37

- 2: Fix double counting potential
(keep same Vdc/n0 at each charge iteration,
n0 to be provided.)
- 1: Standard double counting potential
(n0 self-consistently determined.)
- 0: No double counting.

Please select LDC:

Pick one from [12, 0, 1, 2]...12

Please enter the tolerance of solving the equations of {R, \lambda}
(recommend 1.e-5 or smaller)...5.e-6

LNEWTON = 0: Recommended. Modified Powell hybrid method (HYDRD1).

- 1: Broyden method. Faster for solutions with Z
much larger than 0, e.g., magnetic calculations.

Please select LNEWTON:

Pick one from [-1, 0]...0

LCLUSTER = 0: Single-atom impurity.

- 1: Multi-atom (cluster) impurity.

Please select LCLUSTER:

Pick one from [0, 1]...0

Solution embedding system:

LEIGV = 0: Choose automatically solver depending
on the size of the problem (DEFAULT)

- 1: Exact diagonalization (ZHEEV) in LAPACK
- 2: Lanczos (zhdrv1) in ARPACK
- 3: Exact diagonalization (ZHEEVX,
selective lowest two eigen-vectors) in LAPACK
- 5: PRIMME (Recommended for large dimension.)

Please select LEIGV:

Pick one from [5, 0, 1, 2, 3]...5

INFORMATION FOR f ELECTRONS OF U :
Please provide interaction parameters U,J
separated by a space: 9 0.6

Other questions not related
with symmetry analysis

Provide U,J parameters for atom
indicated (U in this case)

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:...w/test_UO2/LDA/UO2
lanata@rupc04:...w/test_UO2/LDA/UO2 118x37
(n0 self-consistently determined.)
0: No double counting.
Please select LDC:
Pick one from [12, 0, 1, 2]...12

Please enter the tolerance of solving the equations of {R, \lambda}
(recommend 1.e-5 or smaller)...5.e-6

LNEWTON = 0: Recommended. Modified Powell hybrid method (HYDRD1).
-1: Broyden method. Faster for solutions with Z
    much larger than 0, e.g., magnetic calculations.
Please select LNEWTON:
Pick one from [-1, 0]...0

LCLUSTER = 0: Single-atom impurity.
1: Multi-atom (cluster) impurity.
Please select LCLUSTER:
Pick one from [0, 1]...0

Solution embedding system:
LEIGV = 0: Choose automatically solver depending
on the size of the problem (DEFAULT)
1: Exact diagonalization (ZHEEV) in LAPACK
2: Lanczos (zhdrv1) in ARPACK
3: Exact diagonalization (ZHEEVX,
selective lowest two eigen-vectors) in LAPACK
5: PRIMME (Recommended for large dimension.)
Please select LEIGV:
Pick one from [5, 0, 1, 2, 3]...5

INFORMATION FOR f ELECTRONS OF U :
Please provide interaction parameters U,J
separated by a space: 9 0.6
Please provide N1,N2 defining valence range [N1,N2]
separated by a space ( 0 < N1 < N2 < 14 ): 0 4
Please provide guess n0 for valence
(0 < n0 < 4 overwritten by GL_NELF1.INP): 2.1
```

Other questions not related
with symmetry analysis

Relevant valence range of U atom.
Embedding problem computationally
challenging when CFS and SOC both non-
negligible. Valence truncation necessary
with Lanczos (and fortunately licit for this
system).

Initialization UO₂ : LDA + RISB

```
lanata@rupc04:~/w/test_UO2/LDA/UO2
lanata@rupc04:~/w/test_UO2/LDA/UO2 118x37
21 -1.00  0.00 -0.00
   -0.00 -0.00  1.00
   0.00  1.00  0.00
22 -0.00  1.00  0.00
   1.00  0.00 -0.00
   -0.00  0.00 -1.00
23  0.00 -1.00 -0.00
   -1.00 -0.00  0.00
   -0.00  0.00 -1.00
Error in sum_chi2 = 24.0
Please run ga_init_dmft.py with parameters given in init_ga.slog
The default dist_cut for extracting a centered cluster
for symmetry evaluation = 3.9044007499
Molecule extracted O_8 U_13 :
atom   x      y      z    distance
  0  -1.35  -1.35  -1.35    2.3297
  0   1.35   1.35  -1.35    2.3297
  0   1.35  -1.35   1.35    2.3297
  U   -0.00  -2.69  -2.69    3.8044
  0   1.35  -1.35  -1.35    2.3297
  U   2.69   0.00  -2.69    3.8044
  U   2.69  -2.69   0.00    3.8044
  0  -1.35   1.35   1.35    2.3297
  U  -2.69  -0.00  -2.69    3.8044
  0  -1.35   1.35  -1.35    2.3297
  U   0.00   2.69  -2.69    3.8044
  U  -2.69  -2.69   0.00    3.8044
  0  -1.35  -1.35   1.35    2.3297
  U   0.00   0.00   0.00    0.0000
  0   1.35   1.35   1.35    2.3297
  U   2.69   2.69   0.00    3.8044
  U   0.00  -2.69   2.69    3.8044
  U   2.69   0.00   2.69    3.8044
  U  -2.69   2.69   0.00    3.8044
  U  -2.69   0.00   2.69    3.8044
  U   0.00   2.69   2.69    3.8044
lanata@rupc04:~/mnt/w/test_UO2/LDA/UO2> less init_ga.slog
```

Initialization completed.
Corresponding information
given (and part of the
processed information)
dumped in file
“init_ga.slog”.

Hands-on Session: Outline

- α -Ce LDA+SB calculation:
density of state, multiplets histogram, band structure.
- α -Fe LDA+SB spin polarized calculation:
density of state, band structure.
- (Optional) Energy-Volume scan for α -Ce.

Hands-on Session: α -Ce

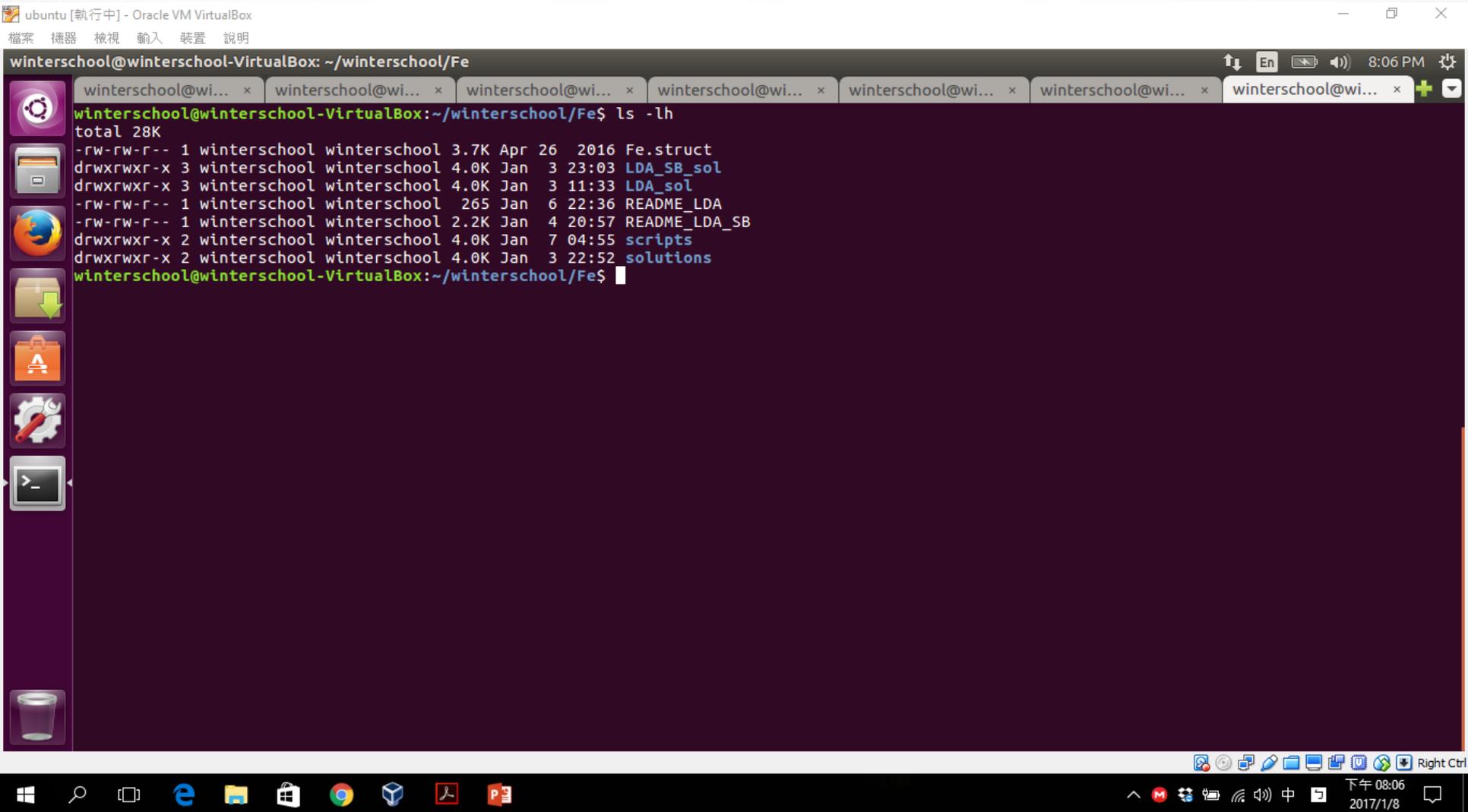
- Perform a LDA+spin orbit calculation with `vxc=5(LDA)`, `numk 5000`, `rkmax=9`.
- Copy the converged LDA folder to LDA+SB and perform a LDA+SB calculation.
- Plot density of state(using `plot_dos.py` in `./scripts`).
- Plot multiplet histogram(using `multiplets_analysis_soc.py` in `./scripts`).
- Perform one shot calculation for band structure with fcc k-path.
- Plot band structure(using `plot_bands.py` in `./scripts`).

Please refer to the README files or

<http://ykent.public.iastate.edu/cygutz/tutorials.html#ce-with-spin-orbit-interaction> for details

Hands-on Session: α -Fe

Folder structure:



The screenshot shows a terminal window titled "winterschool@winterschool-VirtualBox: ~/winterschool/Fe". The terminal displays the output of the command "ls -lh", which lists the files and directories in the current directory. The output is as follows:

```
winterschool@winterschool-VirtualBox: ~/winterschool/Fe$ ls -lh
total 28K
-rw-rw-r-- 1 winterschool winterschool 3.7K Apr 26 2016 Fe.struct
drwxrwxr-x 3 winterschool winterschool 4.0K Jan 3 23:03 LDA_SB_sol
drwxrwxr-x 3 winterschool winterschool 4.0K Jan 3 11:33 LDA_sol
-rw-rw-r-- 1 winterschool winterschool 265 Jan 6 22:36 README_LDA
-rw-rw-r-- 1 winterschool winterschool 2.2K Jan 4 20:57 README_LDA_SB
drwxrwxr-x 2 winterschool winterschool 4.0K Jan 7 04:55 scripts
drwxrwxr-x 2 winterschool winterschool 4.0K Jan 3 22:52 solutions
winterschool@winterschool-VirtualBox:~/winterschool/Fe$
```

The terminal window is part of a virtual machine environment, as indicated by the title bar "ubuntu [執行中] - Oracle VM VirtualBox". The system tray at the bottom right shows the date and time as "下午 08:06 2017/1/8".

Hands-on Session: α -Fe

- Perform a LDA calculation with `vxc=5(LDA)`, `numk 5000`, `rkmax=8`.
- Copy the converged LDA folder to LDA+SB and perform a spin polarized LDA+SB calculation.
- Plot density of state (using `plot_dos.py` in `./scripts`).
- Perform one shot calculation for band structure with bcc k-path.
- Plot band structure (using `plot_bands.py` in `./scripts`).

Please refer to the README files or <http://ykent.public.iastate.edu/cygutz/tutorials.html#ferromagnetic-calculation-for-fe> for details

Hands-on Session: (optional) α -Ce E-V plot

- Change the RMT in Ce.struct to 2.3.
- Create structure files for different volume using gen_struct_folders.py in $\{\text{WIEN_GUTZ_ROOT}\}/\text{tools}/\text{WIEN2k}/$.
- Perform LDA+SB for each volume.
- Plot EV curve using analysis_total_energy.py in $\{\text{WIEN_GUTZ_ROOT}\}/\text{tools}/\text{Gutzwiller}/$.

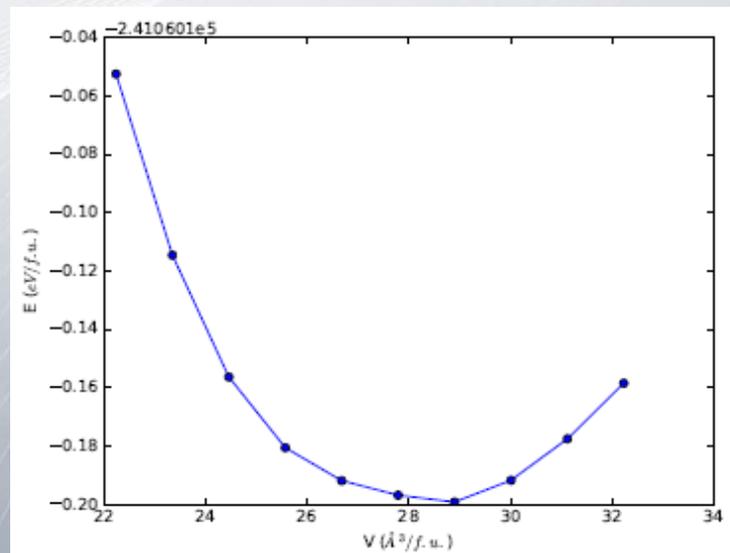
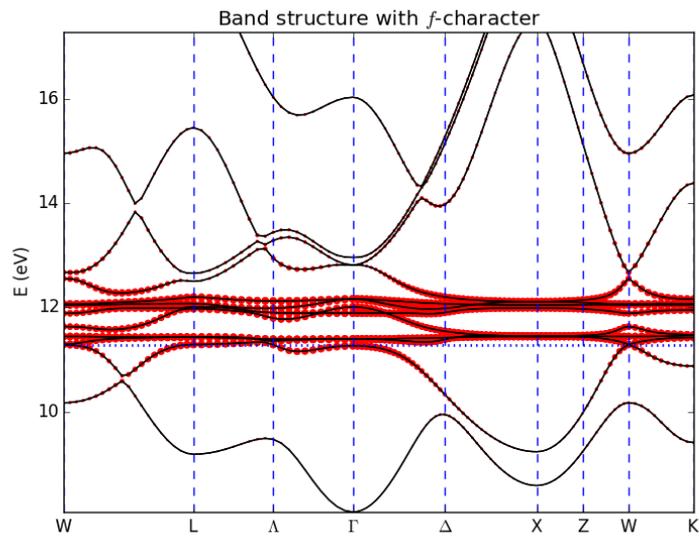
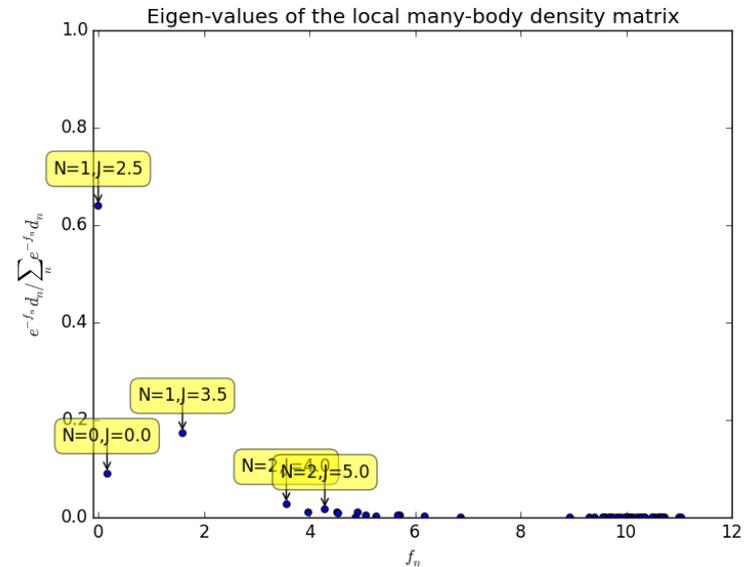
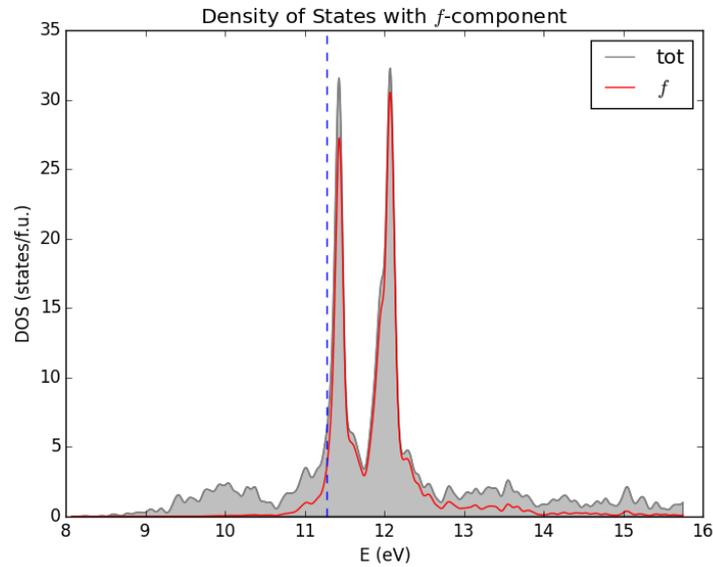
γ - α Isostructural Transition in Cerium, N. Lanata et. al
<http://journals.aps.org/prl/abstract/10.1103/PhysRevLett.111.196801>

Extract important quantities

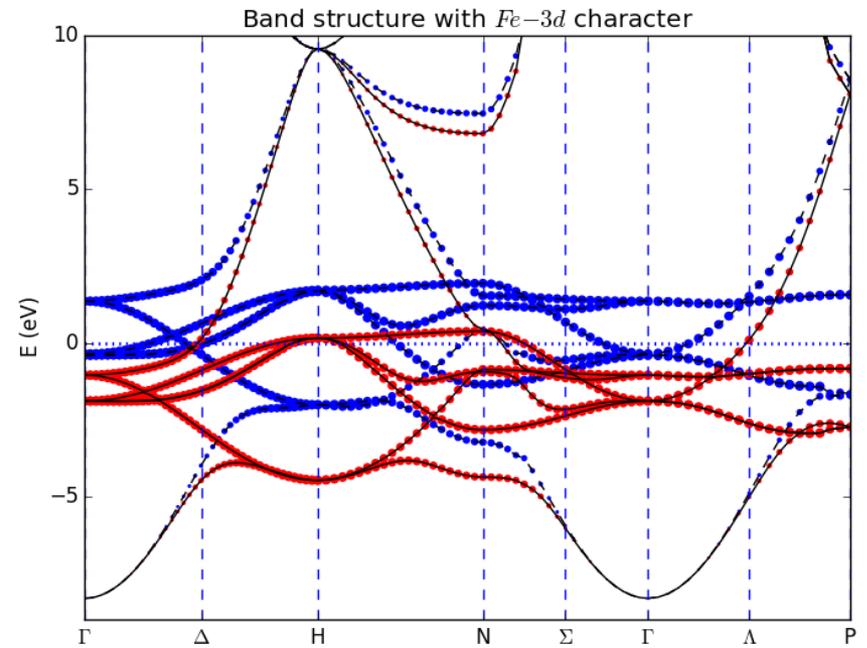
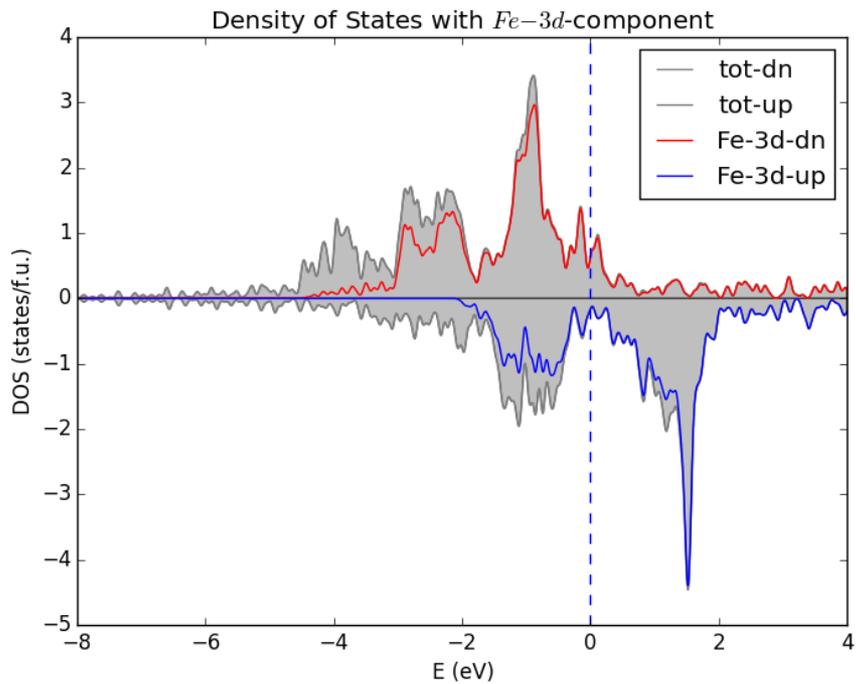
- Total energy: `grep :ENE case.scf`.
- Quasiaprticle weight: `grep -A 26 daggerR GUTZ.LOG`.
- Magnetic moment: `grep MOMENT GUTZ.LOG`.
- Quasiparticle occupancy: `grep -A 26 NKS-UNSYM GUTZ.LOG`
- Physical occupancy: `grep -A 26 NCP_RENORM GUTZ.LOG`.
- Check convergence: `grep :ENE case.dayfile`
- Check CyGutz convergence: `grep MAXERR GUTZ.LOG`.

NOTE: One can `grep` either `GL_LOG.OUT` or `GUTZ.LOG` for CyGutz information.

Hands-on Session: α -Ce



Hands-on Session: α -Fe



Gutzwiller approximation

The variational wavefunction

$$|\Psi_G\rangle = \mathcal{P}|\Psi_0\rangle = \prod_{\mathbf{R}, i \in \text{corr}} \mathcal{P}_{\mathbf{R}i} |\Psi_0\rangle$$

- $|\Psi_0\rangle$: *Slater determinant* (hybridizing bands)
- $\mathcal{P}_{\mathbf{R}i}$: *Local operator* that modifies the weights of the local electronic configurations

$$\mathcal{P}_{\mathbf{R}i} = \sum_{\Gamma n} \lambda_{i, \Gamma n} |\Gamma; \mathbf{R}, i\rangle \langle n; \mathbf{R}, i|$$

Local Fock configurations:

$$|\Gamma; \mathbf{R}, i\rangle = \left(c_{\mathbf{R}i1}^\dagger\right)^{n_1} \cdots \left(c_{\mathbf{R}iM}^\dagger\right)^{n_M} |0\rangle$$

$$|n; \mathbf{R}, i\rangle = \left(f_{\mathbf{R}i1}^\dagger\right)^{n'_1} \cdots \left(f_{\mathbf{R}iM}^\dagger\right)^{n'_M} |0\rangle \quad \left(\langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle \equiv n_{iab}^0 = \delta_{ab} n_{ibb}^0\right)$$

Calculations considerably simplified by the following assumptions:

Gutzwiller Approximation:

$|\Psi_G\rangle$ can be dealt only numerically unless in
the limit of ∞ -coordination lattices
(as in DMFT)

Gutzwiller constraints:

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle = \langle \Psi_0 | \Psi_0 \rangle = 1$$

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle = \langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle \quad (\forall a, b)$$

(“slightly” reduce variational freedom)

Considerable simplification of the calculations

Gutzwiller constraints:

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle = \langle \Psi_0 | \Psi_0 \rangle = 1$$

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle = \langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle \quad (\forall a, b)$$

Key consequence:

$$\begin{aligned} \langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ia} | \Psi_0 \rangle &= \langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle \langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ia} | \Psi_0 \rangle \\ &+ \langle \Psi_0 | \left[\mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} \right] \left(f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ia} \right) | \Psi_0 \rangle_{2\text{-legs contracted}} \end{aligned}$$

$$\langle \Psi_0 | \left[\mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} \right] \left(c_{\mathbf{R}'j\alpha}^\dagger c_{\mathbf{R}'j\alpha} \right) | \Psi_0 \rangle_{2\text{-legs contracted}} = 0 \quad \forall \mathbf{R}, i; \mathbf{R}', j$$

Local operators:

$$\begin{aligned}
\langle \Psi_G | \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] | \Psi_G \rangle &\equiv \langle \Psi_0 | \mathcal{P}^\dagger \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] \mathcal{P} | \Psi_0 \rangle \\
&= \langle \Psi_0 | \left[\prod_{\mathbf{R}', i' \neq \mathbf{R}, i} \mathcal{P}_{\mathbf{R}'i'}^\dagger \mathcal{P}_{\mathbf{R}'i'} \right] \mathcal{P}_{\mathbf{R}i}^\dagger \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle \\
&= \langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle \\
&+ \langle \Psi_0 | \left[\prod_{\mathbf{R}', i' \neq \mathbf{R}', i} \mathcal{P}_{\mathbf{R}'i'}^\dagger \mathcal{P}_{\mathbf{R}'i'} \right] \left(\mathcal{P}_{\mathbf{R}i}^\dagger \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] \mathcal{P}_{\mathbf{R}i} \right) | \Psi_0 \rangle_{2\text{-legs}} \\
&+ \langle \Psi_0 | \left[\prod_{\mathbf{R}', i' \neq \mathbf{R}', i} \mathcal{P}_{\mathbf{R}'i'}^\dagger \mathcal{P}_{\mathbf{R}'i'} \right] \left(\mathcal{P}_{\mathbf{R}i}^\dagger \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] \mathcal{P}_{\mathbf{R}i} \right) | \Psi_0 \rangle_{(N \geq 4)\text{-legs}}
\end{aligned}$$

Local operators:

$$\langle \Psi_0 | \mathcal{P}^\dagger \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] \mathcal{P} | \Psi_0 \rangle = \boxed{\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \hat{O}_{\mathbf{R}i} [c_{\mathbf{R}i\alpha}^\dagger, c_{\mathbf{R}i\alpha}] \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle}$$

Inter-site single-particle quadratic operators:

$$\begin{aligned} \langle \Psi_0 | \mathcal{P}^\dagger c_{\mathbf{R}i\alpha}^\dagger c_{\mathbf{R}'j\beta} \mathcal{P} | \Psi_0 \rangle \\ = \langle \Psi_0 | [\mathcal{P}_{\mathbf{R}i}^\dagger c_{\mathbf{R}i\alpha}^\dagger \mathcal{P}_{\mathbf{R}i}] [\mathcal{P}_{\mathbf{R}'j}^\dagger c_{\mathbf{R}'j\beta} \mathcal{P}_{\mathbf{R}'j}] | \Psi_0 \rangle \end{aligned}$$

where $\mathcal{P}_{\mathbf{R}i} = \sum_{\Gamma n} \lambda_{i,\Gamma n} |\Gamma; \mathbf{R}, i\rangle \langle n; \mathbf{R}, i|$

Inter-site single-particle density matrix operators:

$$\begin{aligned}
 \langle \Psi_0 | \mathcal{P}^\dagger c_{\mathbf{R}i\alpha}^\dagger c_{\mathbf{R}'j\beta} \mathcal{P} | \Psi_0 \rangle &= \langle \Psi_0 | [\mathcal{P}_{\mathbf{R}i}^\dagger c_{\mathbf{R}i\alpha}^\dagger \mathcal{P}_{\mathbf{R}i}] [\mathcal{P}_{\mathbf{R}'j}^\dagger c_{\mathbf{R}'j\beta} \mathcal{P}_{\mathbf{R}'j}] | \Psi_0 \rangle \\
 &= \langle \Psi_0 | [\mathcal{P}_{\mathbf{R}i}^\dagger c_{\mathbf{R}i\alpha}^\dagger \mathcal{P}_{\mathbf{R}i}] [\mathcal{P}_{\mathbf{R}'j}^\dagger c_{\mathbf{R}'j\beta} \mathcal{P}_{\mathbf{R}'j}] | \Psi_0 \rangle_{1\text{-leg}} \\
 &\equiv \sum_{ab} \langle \Psi_0 | \left([\mathcal{R}_i]_{a\alpha} f_{\mathbf{R}ia}^\dagger \right) \left([\mathcal{R}_j]_{b\beta}^* f_{\mathbf{R}'jb} \right) | \Psi_0 \rangle
 \end{aligned}$$

Original ladder operators effectively transform as

$$c_{\mathbf{R}i\alpha}^\dagger \rightarrow \sum_a [\mathcal{R}_i]_{a\alpha} f_{\mathbf{R}ia}^\dagger$$

under the action of the Gutzwiller projector, where:

$$[\mathcal{R}_i]_{a\alpha} = \frac{\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger [c_{\mathbf{R}i\alpha}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia}] | \Psi_0 \rangle}{\langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ia} | \Psi_0 \rangle}$$

$$\mathcal{P}_{\mathbf{R}i} = \sum_{\Gamma n} \lambda_{i,\Gamma n} |\Gamma; \mathbf{R}, i\rangle \langle n; \mathbf{R}, i|$$

Important $|\Psi_0\rangle$ -averages of local operators expressed as traces: step 1

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle = \text{Tr} \left[P_i^0 \lambda_i^\dagger \lambda_i \right] = 1$$

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle = \text{Tr} \left[P_i^0 \lambda_i^\dagger \lambda_i F_{ia}^\dagger F_{ib} \right] = \langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle \equiv n_{iab}^0 \delta_{ab}$$

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger c_{\mathbf{R}i\alpha}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia} | \Psi_0 \rangle = \text{Tr} \left[P_i^0 \lambda_i^\dagger F_{i\alpha}^\dagger \lambda_i F_{ia} \right]$$

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \hat{O}_{\mathbf{R}i} \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle = \text{Tr} \left[P_i^0 \lambda_i^\dagger O \lambda_i \right]$$

$$\mathcal{P}_{\mathbf{R}i} \equiv \sum_{\Gamma n} \lambda_{i,\Gamma n} |\Gamma; \mathbf{R}, i\rangle \langle n; \mathbf{R}, i|$$

$$|\Gamma; \mathbf{R}, i\rangle \equiv \left[c_{\mathbf{R}i1}^\dagger \right]^{n_1} \cdots \left[c_{\mathbf{R}iM}^\dagger \right]^{n_M} |0\rangle; \quad |n; \mathbf{R}, i\rangle \equiv \left[f_{\mathbf{R}i1}^\dagger \right]^{n_1} \cdots \left[f_{\mathbf{R}iM}^\dagger \right]^{n_M} |0\rangle$$

$$\left[P_i^0 \right]_{nn'} \equiv \langle \Psi_0 | |n', \mathbf{R}i\rangle \langle n, \mathbf{R}i| | \Psi_0 \rangle \delta_{nn'}$$

$$\left[F_{ib} \right]_{nn'} = \langle \Gamma, \mathbf{R}i | c_{\mathbf{R}ib} | \Gamma', \mathbf{R}i \rangle = \langle n, \mathbf{R}i | f_{\mathbf{R}ib} | n', \mathbf{R}i \rangle$$

$$\left[O \right]_{\Gamma\Gamma'} = \langle \Gamma, \mathbf{R}i | \hat{O}_{\mathbf{R}i} | \Gamma', \mathbf{R}i \rangle$$

Important $|\Psi_0\rangle$ -averages of local operators expressed as traces: step 2

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle = \text{Tr} [\phi_i \phi_i^\dagger] = 1$$

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle = \text{Tr} [\phi_i^\dagger \phi_i F_{ia}^\dagger F_{ib}] = \langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ib} | \Psi_0 \rangle \equiv n_{iab}^0 \delta_{ab}$$

$$\begin{aligned} [\mathcal{R}_i]_{a\alpha} &\equiv \frac{\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger c_{\mathbf{R}i\alpha}^\dagger \mathcal{P}_{\mathbf{R}i} f_{\mathbf{R}ia} | \Psi_0 \rangle}{\langle \Psi_0 | f_{\mathbf{R}ia}^\dagger f_{\mathbf{R}ia} | \Psi_0 \rangle} \\ &= \text{Tr} [\phi_i^\dagger F_{i\alpha}^\dagger \phi_i F_{ia}] / \sqrt{n_{iaa}^0 (1 - n_{iaa}^0)} \end{aligned}$$

$$\langle \Psi_0 | \mathcal{P}_{\mathbf{R}i}^\dagger \hat{O}_{\mathbf{R}i} \mathcal{P}_{\mathbf{R}i} | \Psi_0 \rangle = \text{Tr} [\phi_i \phi_i^\dagger O]$$

$$\mathcal{P}_{\mathbf{R}i} \equiv \sum_{\Gamma n} \lambda_{i,\Gamma n} |\Gamma; \mathbf{R}, i\rangle \langle n; \mathbf{R}, i|$$

$$[P_i^0]_{nn'} \equiv \langle \Psi_0 | |n', Ri\rangle \langle n, Ri| | \Psi_0 \rangle \delta_{nn'}$$

$$[F_{ib}]_{nn'} = \langle \Gamma, Ri | c_{Rib} | \Gamma', Ri \rangle = \langle n, Ri | f_{Rib} | n', Ri \rangle$$

$$[O]_{\Gamma\Gamma'} = \langle \Gamma, Ri | \hat{O}_{\mathbf{R}i} | \Gamma', Ri \rangle$$

$$[\phi_i] = \lambda_i \sqrt{P_i^0}$$

**Initialization UO_2 :
LDA + RISB Mott**

Initialization UO₂ : LDA + RISB Mott

```
henhans@henhans-Satellite-C55-C: ~ × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × henhans@henhans-Satellite-C55-C: ~/cyg... ×  
[thlee@zakynthos UO2]$ python ${WIEN_GUTZ_ROOT}/tools/Gutzwiller/init_mott.py
```

Initialization UO₂ : LDA + RISB Mott

henhans@henhans-Satellite-C55-C: ~ × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × henhans@henhans-Satellite-C55-C: ~/cyg...

```
[thlee@zakynthos UO2]$ python ${WIEN_GUTZ_ROOT}/tools/Gutzwiller/init_mott.py
```

```
***** Impurity 0 *****
```

```
Sigma structure:
```

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	1	2	0	0	0	0	0	0	0	0	0	0	0	0
1	3	4	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	1	2	0	0	0	0	0	0	0	0	0	0
3	0	0	3	4	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	5	6	0	0	0	0	0	0	0	0
5	0	0	0	0	7	8	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	5	6	0	0	0	0	0	0
7	0	0	0	0	0	0	7	8	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	5	6	0	0	0	0
9	0	0	0	0	0	0	0	0	7	8	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	5	6	0	0
11	0	0	0	0	0	0	0	0	0	0	7	8	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	9	0
13	0	0	0	0	0	0	0	0	0	0	0	0	0	9

```
Please provide the indices of orbitals to be Mott localized
```

```
(e.g., 0 2 ): 4 6 8 10
```

Initialization UO₂ : LDA + RISB Mott

```
henhans@henhans-Satellite-C55-C: ~ × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × henhans@henhans-Satellite-C55-C: ~/cyg... ×
[thlee@zakynthos UO2]$ python ${WIEN_GUTZ_ROOT}/tools/Gutzwiller/init_mott.py
***** Impurity 0 *****
Sigma structure:
index    0    1    2    3    4    5    6    7    8    9   10   11   12   13
  0      1    2    0    0    0    0    0    0    0    0    0    0    0
  1      3    4    0    0    0    0    0    0    0    0    0    0    0
  2      0    0    1    2    0    0    0    0    0    0    0    0    0
  3      0    0    3    4    0    0    0    0    0    0    0    0    0
  4      0    0    0    0    5    6    0    0    0    0    0    0    0
  5      0    0    0    0    7    8    0    0    0    0    0    0    0
  6      0    0    0    0    0    0    5    6    0    0    0    0    0
  7      0    0    0    0    0    0    7    8    0    0    0    0    0
  8      0    0    0    0    0    0    0    0    5    6    0    0    0
  9      0    0    0    0    0    0    0    0    7    8    0    0    0
 10      0    0    0    0    0    0    0    0    0    0    5    6    0    0
 11      0    0    0    0    0    0    0    0    0    0    7    8    0    0
 12      0    0    0    0    0    0    0    0    0    0    0    0    9    0
 13      0    0    0    0    0    0    0    0    0    0    0    0    0    9
Please provide the indices of orbitals to be Mott localized
(e.g., 0 2 ): 4 6 8 10
You selected [4 6 8 10] to be Mott localized, right? (y/n):y
```

Initialization UO₂ : LDA + RISB Mott

henhans@henhans-Satellite-C55-C: ~ × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × henhans@henhans-Satellite-C55-C: ~/cyg... ×

```
[thlee@zakynthos UO2]$ python ${WIEN_GUTZ_ROOT}/tools/Gutzwiller/init_mott.py
```

```
***** Impurity 0 *****
```

```
Sigma structure:
```

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	1	2	0	0	0	0	0	0	0	0	0	0	0	0
1	3	4	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	1	2	0	0	0	0	0	0	0	0	0	0
3	0	0	3	4	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	5	6	0	0	0	0	0	0	0	0
5	0	0	0	0	7	8	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	5	6	0	0	0	0	0	0
7	0	0	0	0	0	0	7	8	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	5	6	0	0	0	0
9	0	0	0	0	0	0	0	7	8	0	0	0	0	0
10	0	0	0	0	0	0	0	0	0	5	6	0	0	0
11	0	0	0	0	0	0	0	0	0	7	8	0	0	0
12	0	0	0	0	0	0	0	0	0	0	0	9	0	0
13	0	0	0	0	0	0	0	0	0	0	0	0	9	0

```
Please provide the indices of orbitals to be Mott localized
```

```
(e.g., 0 2 ): 4 6 8 10
```

```
You selected [4 6 8 10] to be Mott localized, right? (y/n):y
```

```
Please provide the total number of Mott localized electrons (per unit cell): 2
```

Initialization UO₂ : LDA + RISB Mott

henhans@henhans-Satellite-C55-C: ~ × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × henhans@henhans-Satellite-C55-C: ~/cyg... ×

```
[thlee@zakynthos UO2]$ python ${WIEN_GUTZ_ROOT}/tools/Gutzwiller/init_mott.py
```

```
***** Impurity 0 *****
```

```
Sigma structure:
```

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	1	2	0	0	0	0	0	0	0	0	0	0	0	0
1	3	4	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	1	2	0	0	0	0	0	0	0	0	0	0
3	0	0	3	4	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	5	6	0	0	0	0	0	0	0	0
5	0	0	0	0	7	8	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	5	6	0	0	0	0	0	0
7	0	0	0	0	0	0	7	8	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	5	6	0	0	0	0
9	0	0	0	0	0	0	0	7	8	0	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	5	6	0	0
11	0	0	0	0	0	0	0	0	0	0	7	8	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	9	0
13	0	0	0	0	0	0	0	0	0	0	0	0	0	9

```
Please provide the indices of orbitals to be Mott localized
```

```
(e.g., 0 2 ): 4 6 8 10
```

```
You selected [4 6 8 10] to be Mott localized, right? (y/n):y
```

```
Please provide the total number of Mott localized electrons (per unit cell): 2
```

```
Total 2 electrons will be Mott localized, right? (y/n):y
```

Initialization UO₂ : LDA + RISB Mott

henhans@henhans-Satellite-C55-C: ~ × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × thlee@zakynthos:~/cygutz/UO2/LDA_SB... × henhans@henhans-Satellite-C55-C: ~/cyg...

```
(e.g., 0 2 ): 4 6 8 10
You selected [4 6 8 10] to be Mott localized, right? (y/n):y
Please provide the total number of Mott localized electrons (per unit cell): 2
Total 2 electrons will be Mott localized, right? (y/n):y
```

R structure:

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	1	2	0	0	0	0	0	0	0	0	0	0	0	0
1	3	4	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	1	2	0	0	0	0	0	0	0	0	0	0
3	0	0	3	4	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	5	0	0	0	0	0	0	0	0	0
5	0	0	0	0	6	7	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	5	0	0	0	0	0	0	0
7	0	0	0	0	0	0	6	7	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	5	0	0	0	0	0
9	0	0	0	0	0	0	0	0	6	7	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	5	0	0	0
11	0	0	0	0	0	0	0	0	0	0	6	7	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	8	0
13	0	0	0	0	0	0	0	0	0	0	0	0	0	8

Lambda structure:

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	1	2	0	0	0	0	0	0	0	0	0	0	0	0
1	3	4	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	1	2	0	0	0	0	0	0	0	0	0	0
3	0	0	3	4	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	5	0	0	0	0	0	0	0	0	0
5	0	0	0	0	0	6	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	5	0	0	0	0	0	0	0
7	0	0	0	0	0	0	0	6	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	5	0	0	0	0	0
9	0	0	0	0	0	0	0	0	0	6	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	5	0	0	0
11	0	0	0	0	0	0	0	0	0	0	0	6	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	7	0
13	0	0	0	0	0	0	0	0	0	0	0	0	0	7

```
[thlee@zakynthos UO2]$ python ${WIEN_GUTZ_ROOT}/ga_run_dmft.py
```

**Initialization UO₂:
LDA + RISB Mott (DOS Band Structure)**

Initialization UO_2 : LDA + RISB Mott (DOS Band Structure)

```
henhans@henhans-Satel... x henhans@henhans-Satel... x henhans@henhans-Satel... x henhans@henhans-Satel... x henhans@henhans-Satel... x henhans@henhans-Satel... x  
henhans@henhans-Satellite-C55-C:~/cygutz/U02/LDA_SB_Mott_k2000/U02$ ${WIEN_GUTZ_ROOT}/tools/Gutzwiller/save_lapwg -a -d U02_SCF
```

Initialization UO₂ : LDA + RISB Mott (DOS Band Structure)

```
henhans@henha... x henhans@henha... x
U02.nmat_only -> Ce_SCF/U02.nmat_only
U02.vsp -> Ce_SCF/U02.vsp
U02.vspup -> Ce_SCF/U02.vspup
U02.vspdn -> Ce_SCF/U02.vspdn
U02.r2v -> Ce_SCF/U02.r2v
U02.r2vdn -> Ce_SCF/U02.r2vdn
params.dat -> Ce_SCF/params.dat
EFLDA.INP -> Ce_SCF/EFLDA.INP
EFLDA.OUT -> Ce_SCF/EFLDA.OUT
WH_HS.INP -> Ce_SCF/WH_HS.INP
WH_HS_L.INP -> Ce_SCF/WH_HS_L.INP
WH_HS_R.INP -> Ce_SCF/WH_HS_R.INP
WH_N2N.INP -> Ce_SCF/WH_N2N.INP
WH_RLNEF.INP -> Ce_SCF/WH_RLNEF.INP
WH_SIGMA_STRUCT.INP -> Ce_SCF/WH_SIGMA_STRUCT.INP
WH_SIGMA_STRUCT_L.INP -> Ce_SCF/WH_SIGMA_STRUCT_L.INP
WH_SIGMA_STRUCT_R.INP -> Ce_SCF/WH_SIGMA_STRUCT_R.INP
WH_SL_VEC.INP -> Ce_SCF/WH_SL_VEC.INP
WH_EL0.OUT -> Ce_SCF/WH_EL0.OUT
WH_RLNEF.OUT -> Ce_SCF/WH_RLNEF.OUT
GL.INP -> Ce_SCF/GL.INP
GL_NELF1.INP -> Ce_SCF/GL_NELF1.INP
GMPI_0.INP -> Ce_SCF/GMPI_0.INP
GUTZ1.INP -> Ce_SCF/GUTZ1.INP
GUTZ2.INP -> Ce_SCF/GUTZ2.INP
GUTZ3.INP -> Ce_SCF/GUTZ3.INP
GUTZ4.INP -> Ce_SCF/GUTZ4.INP
GUTZ5.INP -> Ce_SCF/GUTZ5.INP
GL_LOG.OUT -> Ce_SCF/GL_LOG.OUT
GL_NELF1.OUT -> Ce_SCF/GL_NELF1.OUT
GLPJC_1.OUT -> Ce_SCF/GLPJC_1.OUT
FROZEN.INP -> Ce_SCF/FROZEN.INP
glog.h5 -> Ce_SCF/glog.h5
init_ga_info.h5 -> Ce_SCF/init_ga_info.h5
```

broyden files deleted, clm*, dmat*, vorb*, vresp*, eece*, scf, struct and input files saved under Ce_SCF/init_ga_info

```
henhans@henhans-Satellite-C55-C:~/cygutuz/U02/LDA_SB_Mott_k2000/U02$ sed -i 's/*.LSCF.*/LSCF = 2/' GL.INP && sed -i 's/*.LSCF.*/&\nLEL0 = 1/' GL
.INP && sed -i 's/*.LSCF.*/&\nLEFERMI = 1/' GL.INP
```

Initialization UO₂ : LDA + RISB Mott (DOS Band Structure)

```
henhans@henha... x henhans@henha... x
UO2.vsp -> Ce_SCF/UO2.vsp
UO2.vspup -> Ce_SCF/UO2.vspup
UO2.vspd -> Ce_SCF/UO2.vspd
UO2.r2v -> Ce_SCF/UO2.r2v
UO2.r2v -> Ce_SCF/UO2.r2v
params.dat -> Ce_SCF/params.dat
EFLDA.INP -> Ce_SCF/EFLDA.INP
EFLDA.OUT -> Ce_SCF/EFLDA.OUT
WH_HS.INP -> Ce_SCF/WH_HS.INP
WH_HS_L.INP -> Ce_SCF/WH_HS_L.INP
WH_HS_R.INP -> Ce_SCF/WH_HS_R.INP
WH_N2N.INP -> Ce_SCF/WH_N2N.INP
WH_RLNEF.INP -> Ce_SCF/WH_RLNEF.INP
WH_SIGMA_STRUCT.INP -> Ce_SCF/WH_SIGMA_STRUCT.INP
WH_SIGMA_STRUCT_L.INP -> Ce_SCF/WH_SIGMA_STRUCT_L.INP
WH_SIGMA_STRUCT_R.INP -> Ce_SCF/WH_SIGMA_STRUCT_R.INP
WH_SL_VEC.INP -> Ce_SCF/WH_SL_VEC.INP
WH_EL0.OUT -> Ce_SCF/WH_EL0.OUT
WH_RLNEF.OUT -> Ce_SCF/WH_RLNEF.OUT
GL.INP -> Ce_SCF/GL.INP
GL_NELF1.INP -> Ce_SCF/GL_NELF1.INP
GMPI_0.INP -> Ce_SCF/GMPI_0.INP
GUTZ1.INP -> Ce_SCF/GUTZ1.INP
GUTZ2.INP -> Ce_SCF/GUTZ2.INP
GUTZ3.INP -> Ce_SCF/GUTZ3.INP
GUTZ4.INP -> Ce_SCF/GUTZ4.INP
GUTZ5.INP -> Ce_SCF/GUTZ5.INP
GL_LOG.OUT -> Ce_SCF/GL_LOG.OUT
GL_NELF1.OUT -> Ce_SCF/GL_NELF1.OUT
GLPJC_1.OUT -> Ce_SCF/GLPJC_1.OUT
FROZEN.INP -> Ce_SCF/FROZEN.INP
glog.h5 -> Ce_SCF/glog.h5
init_ga_info.h5 -> Ce_SCF/init_ga_info.h5
```

broyden files deleted, clm*, dmat*, vorb*, vresp*, eece*, scf, struct and input files saved under Ce_SCF/init_ga_info

```
henhans@henhans-Satellite-C55-C:~/cygutuz/UO2/LDA_SB_Mott_k2000/UO2$ sed -i 's/.LSCF./LSCF = 2/' GL.INP && sed -i 's/.LSCF./&\nLEL0 = 1/' GL
.INP && sed -i 's/.LSCF./&\nLEFERMI = 1/' GL.INP
```

```
henhans@henhans-Satellite-C55-C:~/cygutuz/UO2/LDA_SB_Mott_k2000/UO2$ cp WH_EL0.OUT WH_EL0.INP && cp EFLDA.OUT EFLDA.INP
```

Initialization UO_2 : LDA + RISB Mott (DOS Band Structure)

```
henhans@henha... ×  
henhans@henhans-Satellite-C55-C:~/cygutz/U02/LDA_SB_Mott_k2000/U02$ cp band_kpts/U02.klist .
```

Initialization UO₂ : LDA + RISB Mott (DOS Band Structure)

```
henhans@henha... × henhans@henha... ×
henhans@henhans-Satellite-C55-C:~/cygutz/U02/LDA_SB_Mott_k2000/U02$ cp band_kpts/U02.klist .
henhans@henhans-Satellite-C55-C:~/cygutz/U02/LDA_SB_Mott_k2000/U02$ ${WIEN_GUTZ_ROOT}/ga_run_dmft.py -s lapw1 -e CyGutz
```